

# Nonlinearly Weighted First-order Regression for Denoising MC Renderings

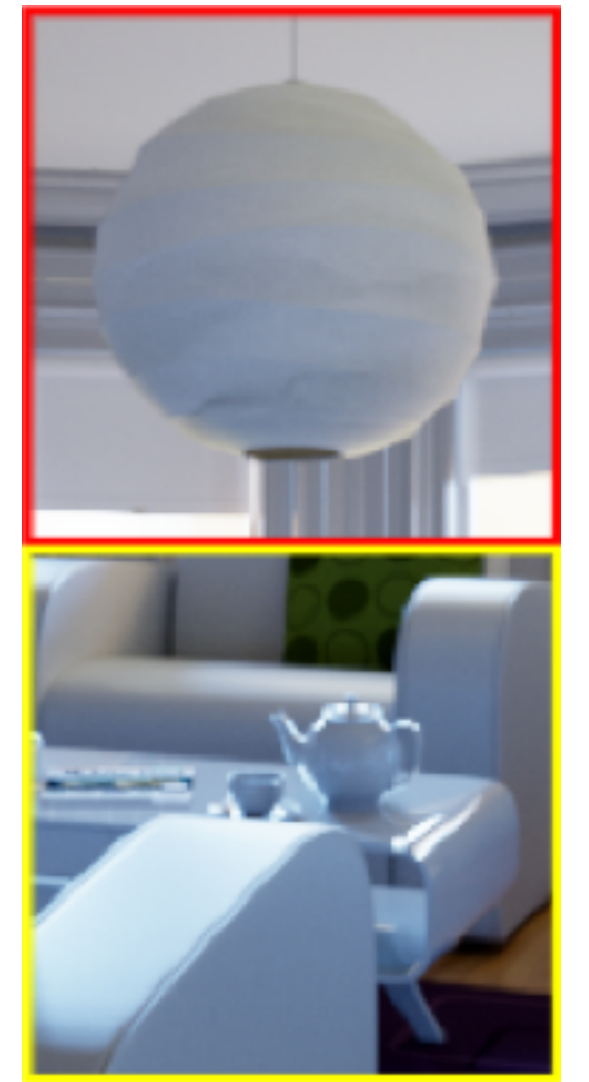
Benedikt Bitterli  
Fabrice Rousselle  
Bochang Moon  
José A. Iglesias-Guitián  
Kenny Mitchell  
David Adler  
Wojciech Jarosz  
Jan Novák



# Goal: study the state of the art



Input



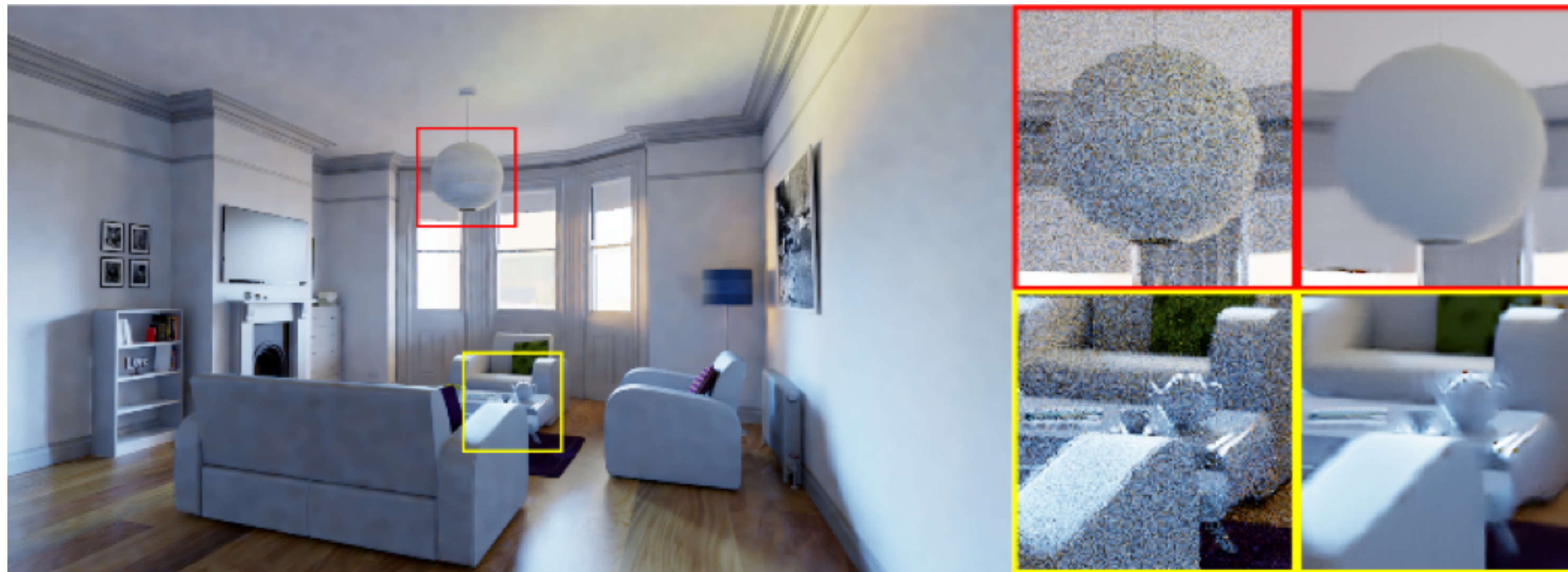
Reference



# Goal: study the state of the art

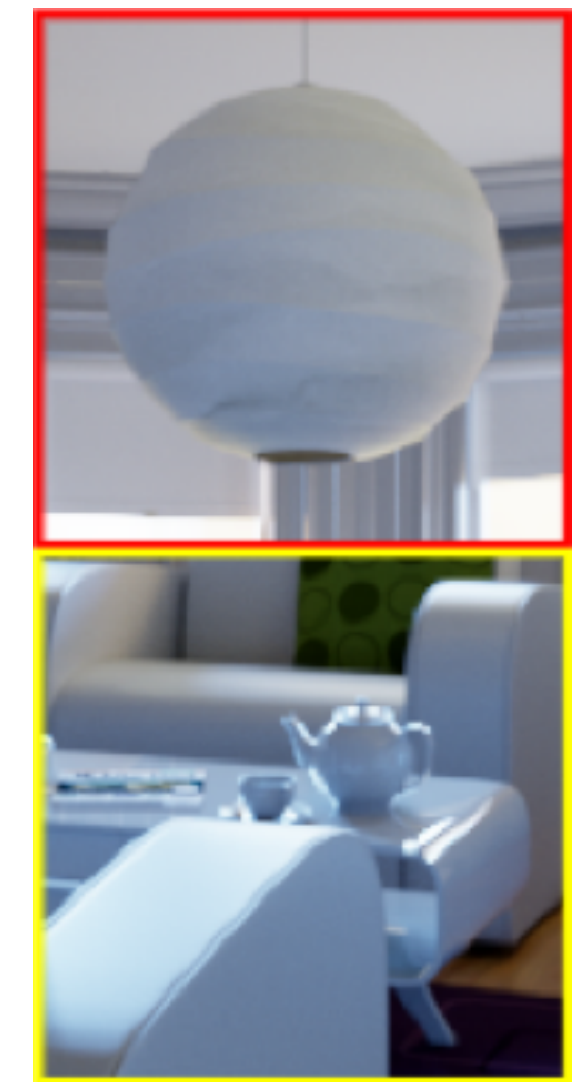
## RHF

Delbracio et al.  
[2014]



Input

RHF



Reference



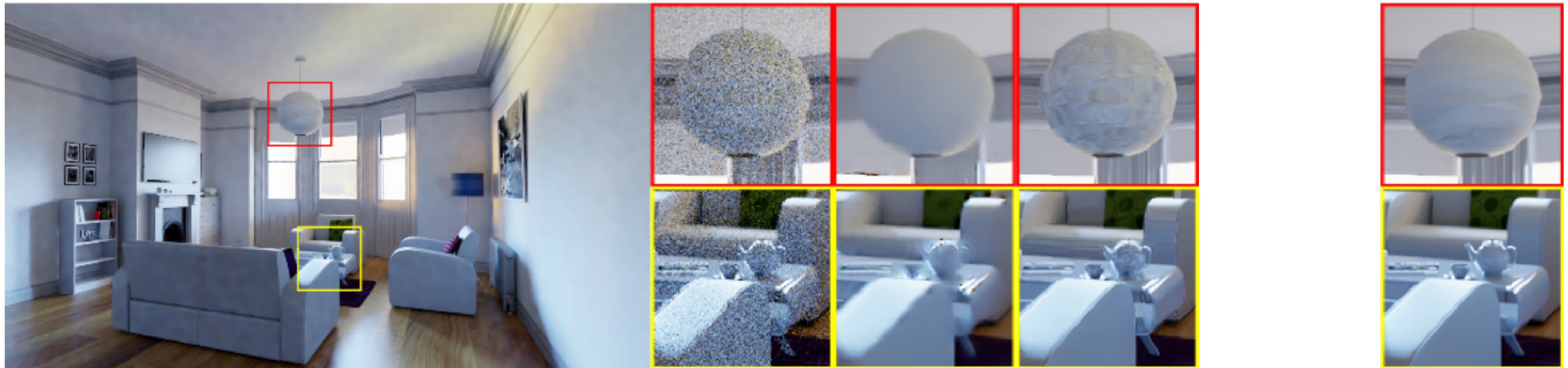
# Goal: study the state of the art

## RHF

Delbracio et al.  
[2014]

## RDFC

Rousselle et al. [2013]



Input

RHF

RDFC

Reference



# Goal: study the state of the art

## RHF

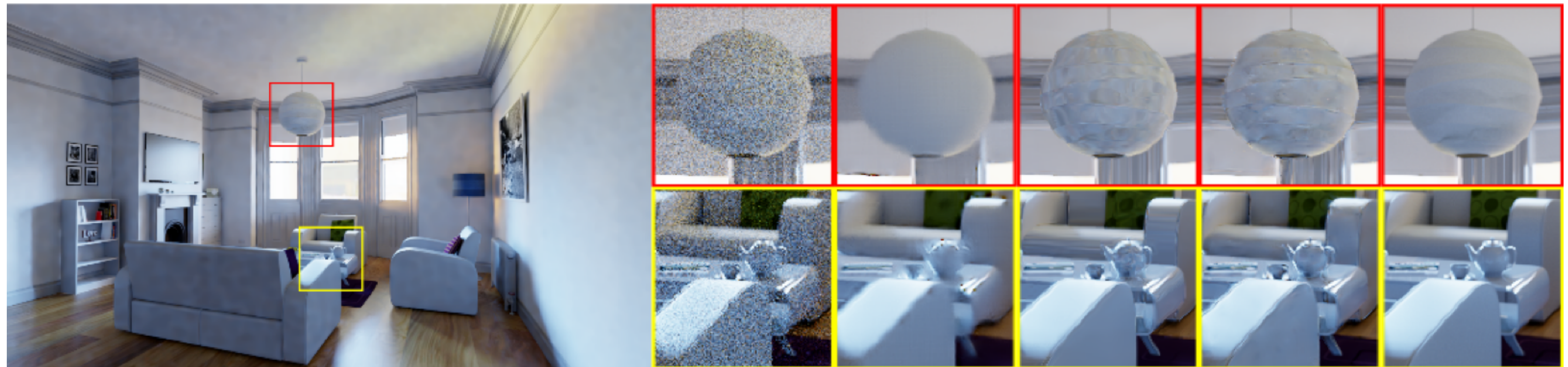
Delbracio et al.  
[2014]

## RDFC

Rousselle et al. [2013]

## WLR

Moon et al. [2014]



Input

RHF

RDFC

WLR

Reference



# Evaluation Criteria

## Essential

Effectiveness – significant noise reduction

Predictability – no manual tuning

Stability – flicker-free results

# Evaluation Criteria

## Essential

Effectiveness – significant noise reduction

Predictability – no manual tuning

Stability – flicker-free results

## Required for Production

Ease of adoption – no intrusive or expensive changes

Speed – significantly faster than rendering

Memory – significantly less than rendering



# No Silver Bullet

RHF

Too blurry, needs manual tuning





# No Silver Bullet

RDFC

Banding artifacts





# No Silver Bullet

WLR

Residual noise





# Methodology

**Theoretical analysis** – how are previous filters related

**Comparative analysis** – how do previous filters perform

**New design** – how can we combine the strengths of previous filters



# Filtering Framework



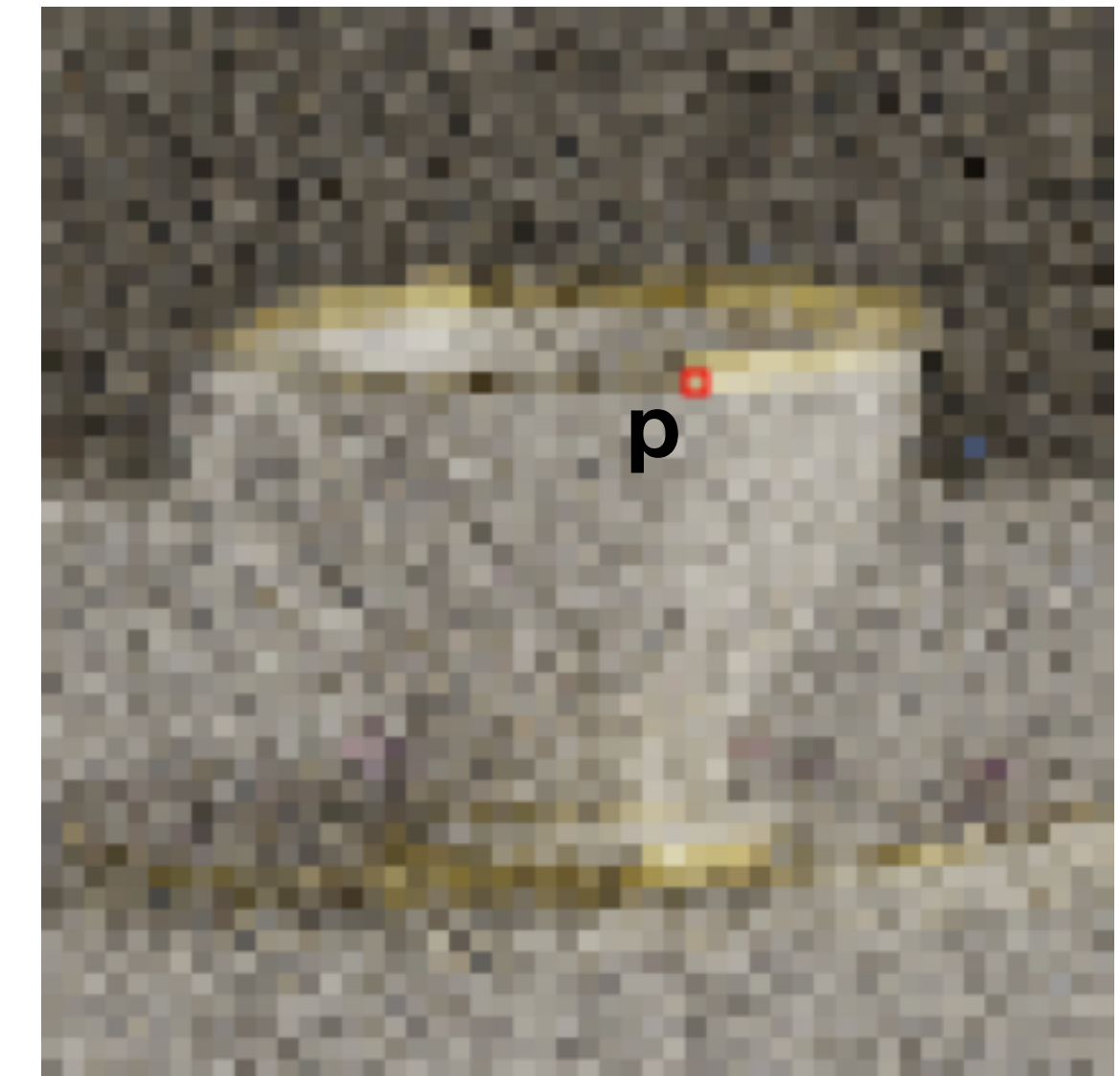
256'000 spp

# Filtering Framework



256 spp

# Filtering Framework



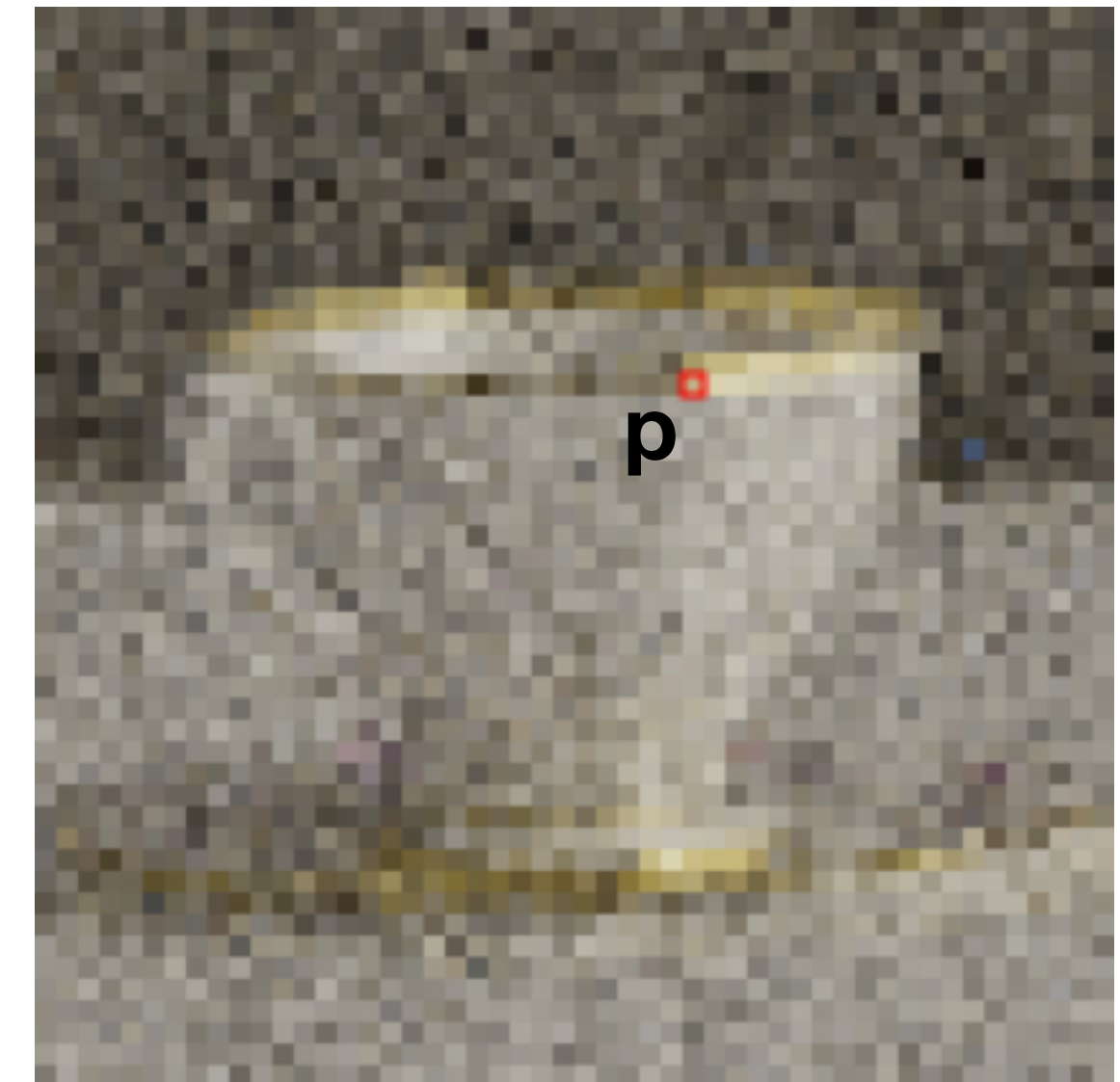
256 spp



# Filtering Framework

All filters perform a regression to minimize

$$\text{Error}(\hat{c}_p) =$$

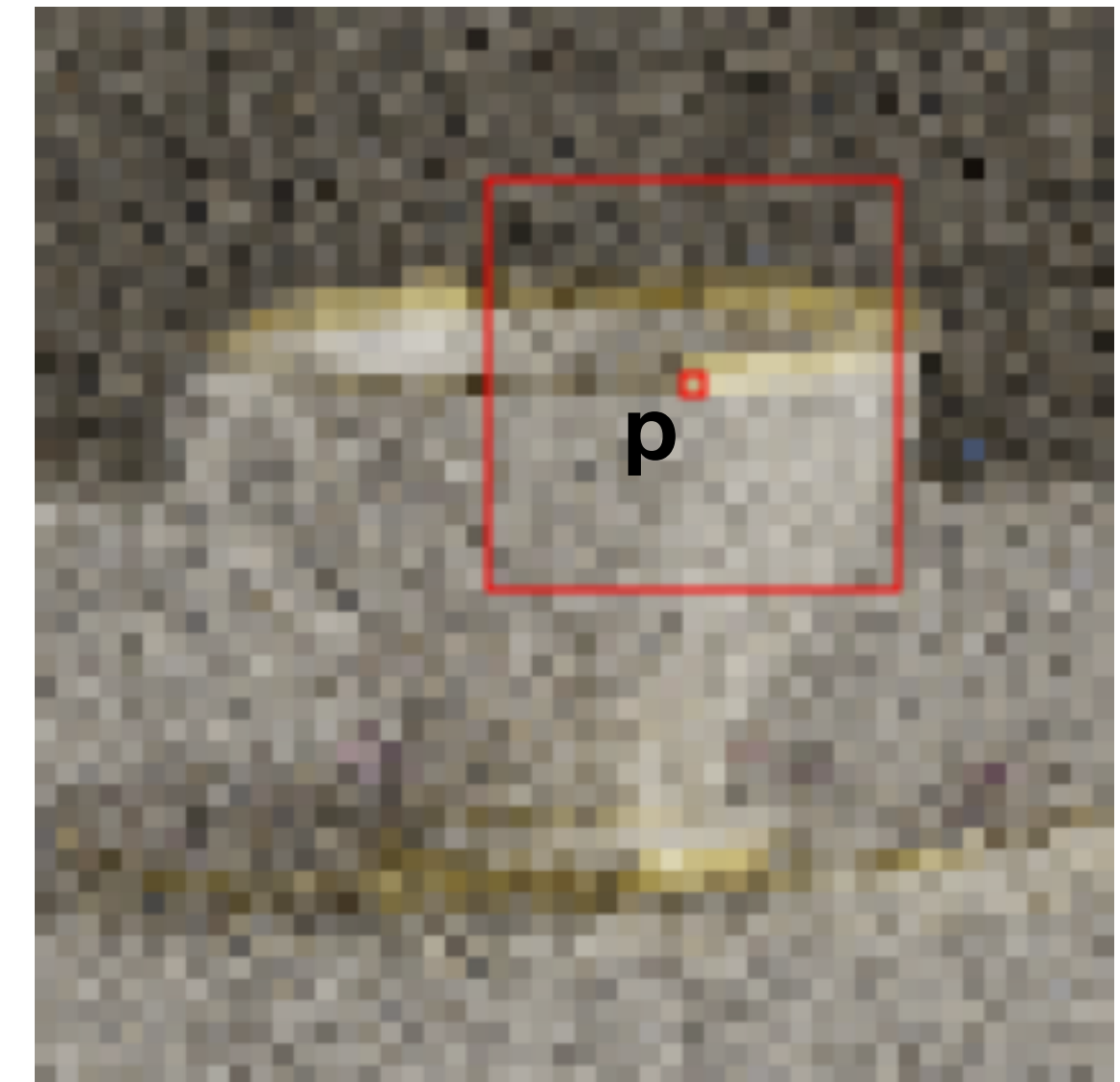


256 spp

# Filtering Framework

All filters perform a regression to minimize

$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p}$$



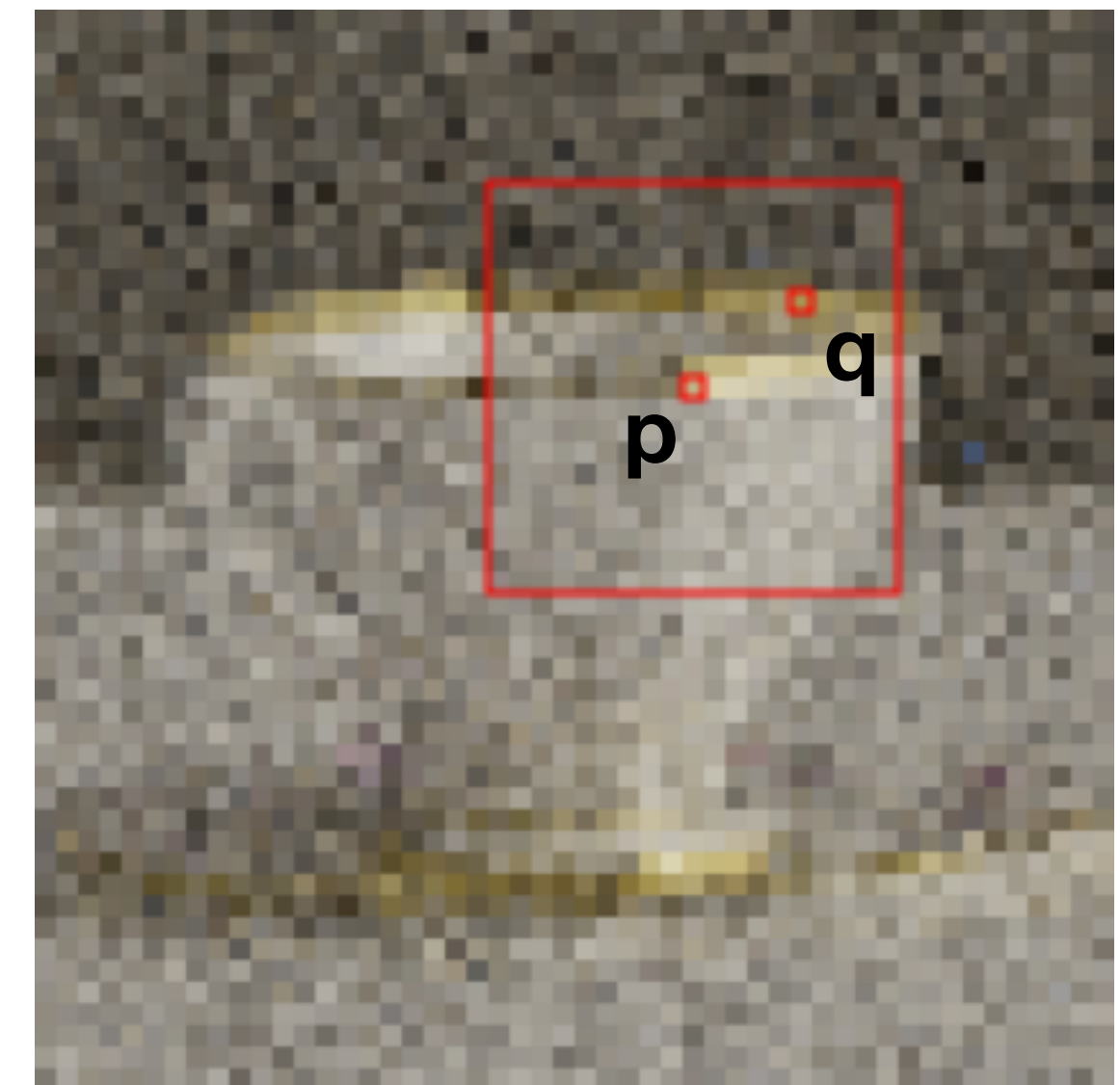
256 spp



# Filtering Framework

All filters perform a regression to minimize

$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_x(p, q))^2$$

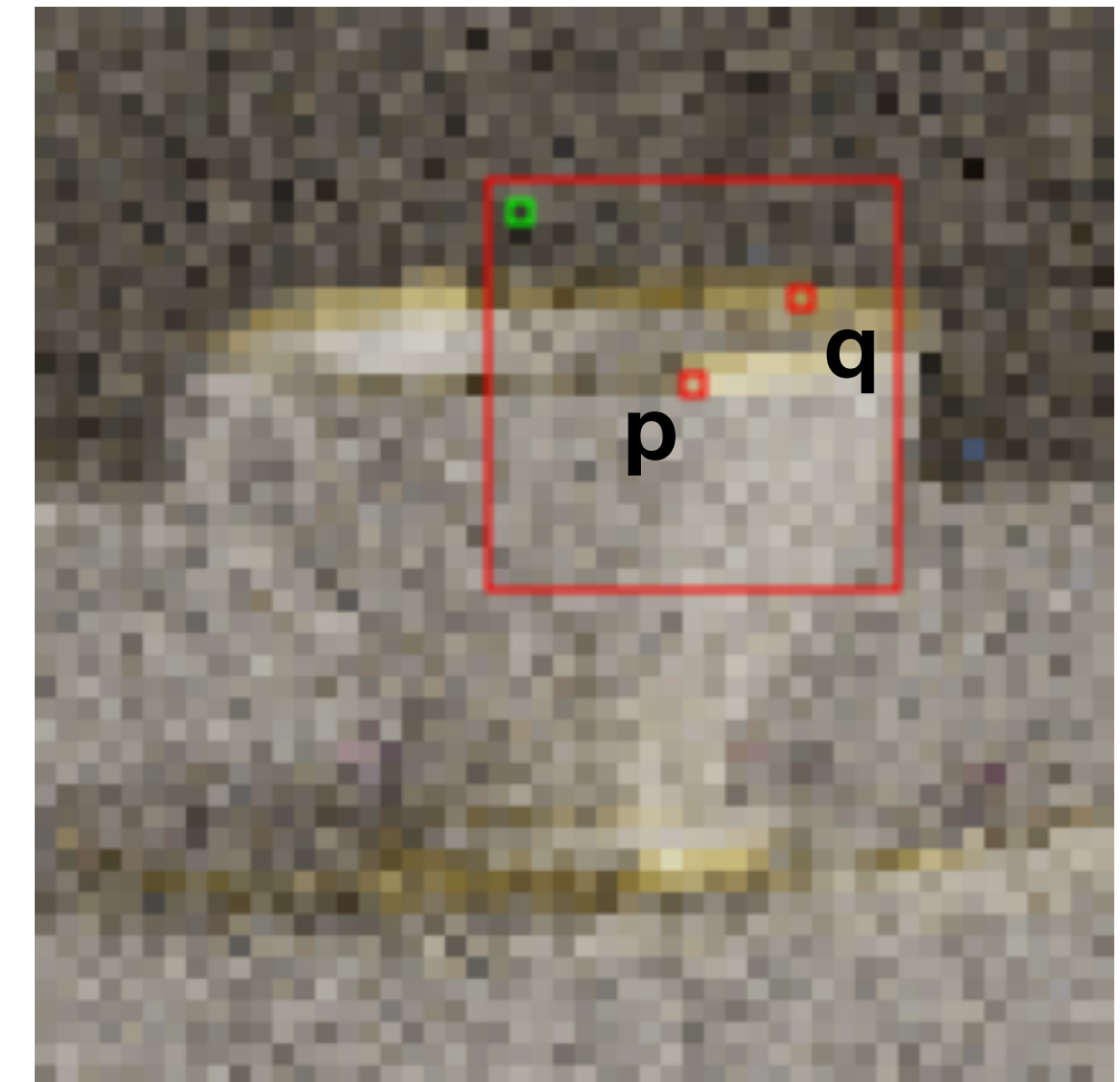


256 spp

# Filtering Framework

All filters perform a regression to minimize

$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$



256 spp

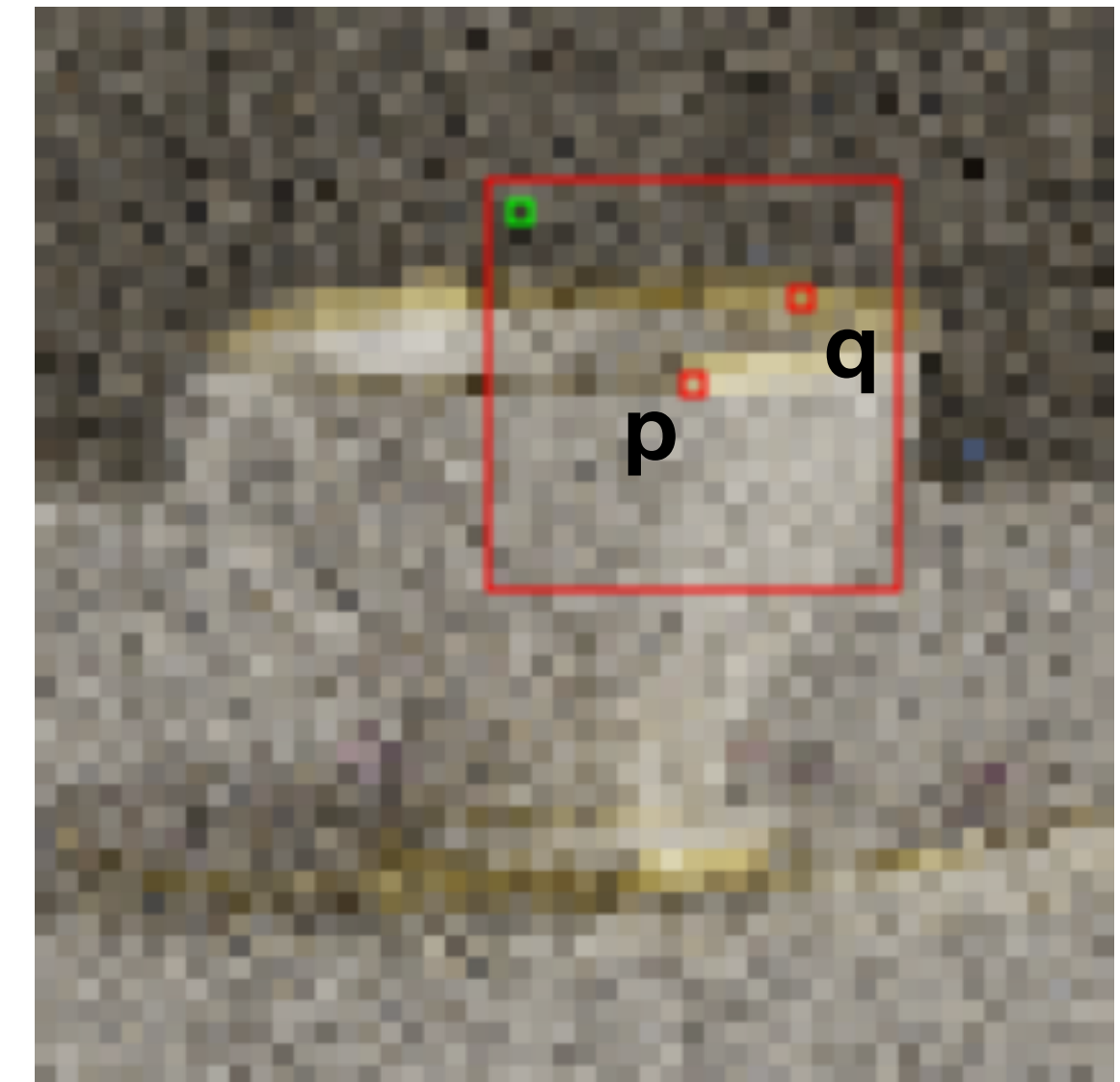


# Filtering Framework

All filters perform a regression to minimize

$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

What **model** and **weights**?

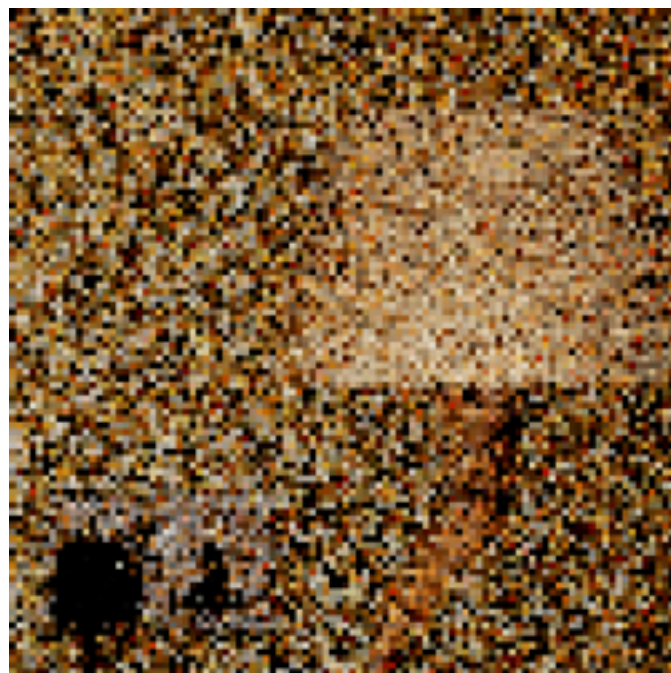


256 spp

# Filtering Framework

$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

Input – 256 spp



Reference





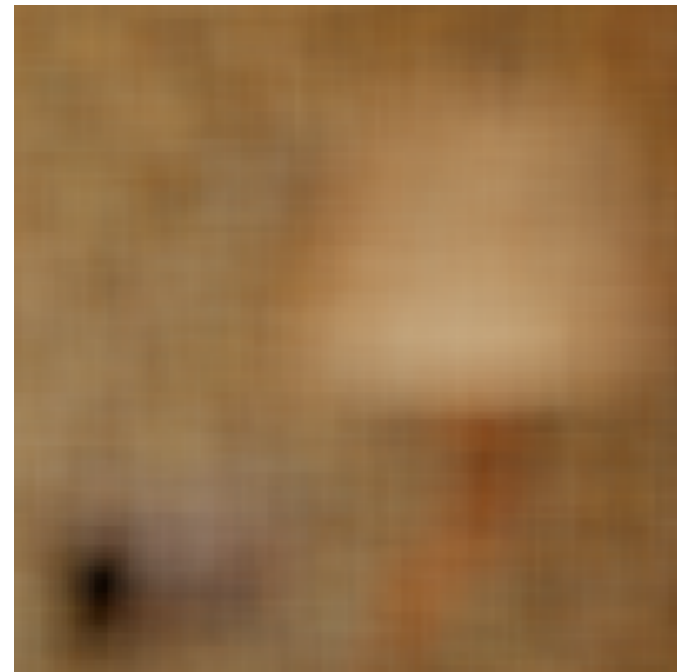
# Filtering Framework — Box Filter

$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

Input – 256 spp



Box Filter



Reference



# Filtering Framework — Box Filter

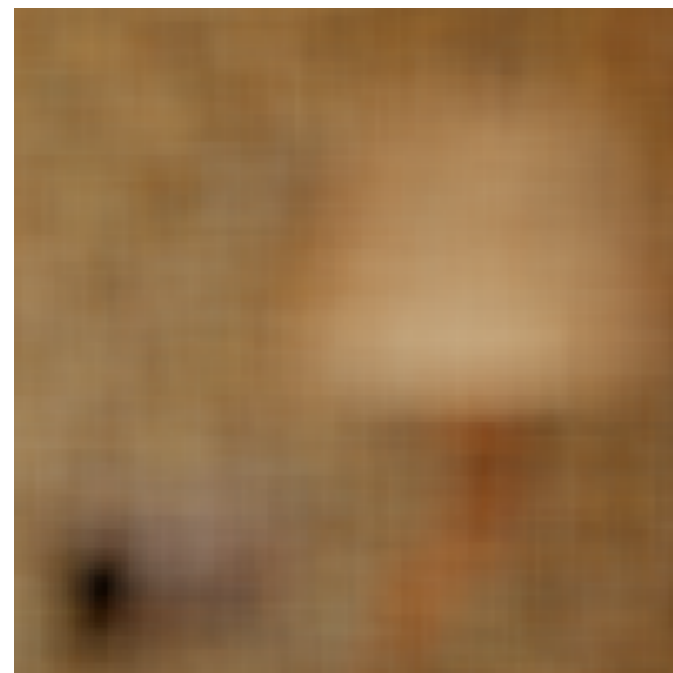
$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

$$\text{Box: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p)^2$$

Input – 256 spp



Box Filter



Reference





# Filtering Framework — Box Filter

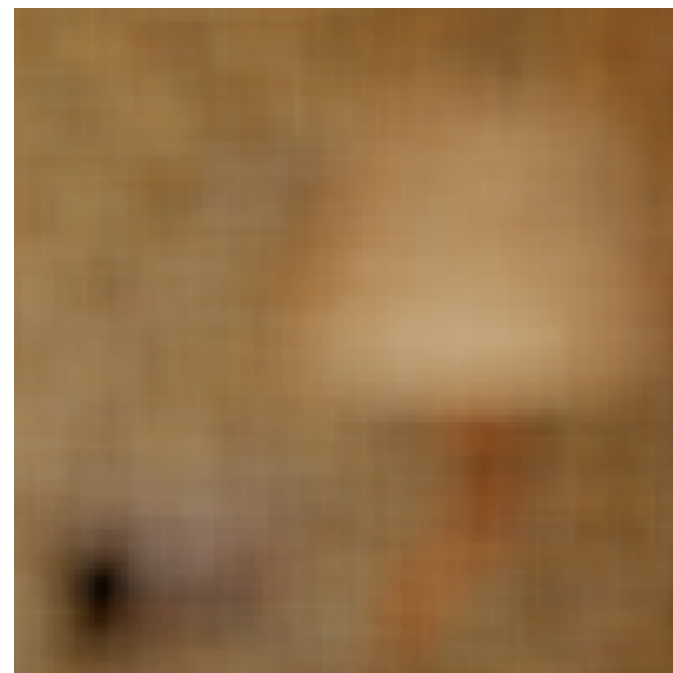
$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

$$\text{Box: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p)^2$$

Input – 256 spp



Box Filter



Weights:

Uniform

Reference



# Filtering Framework — Box Filter

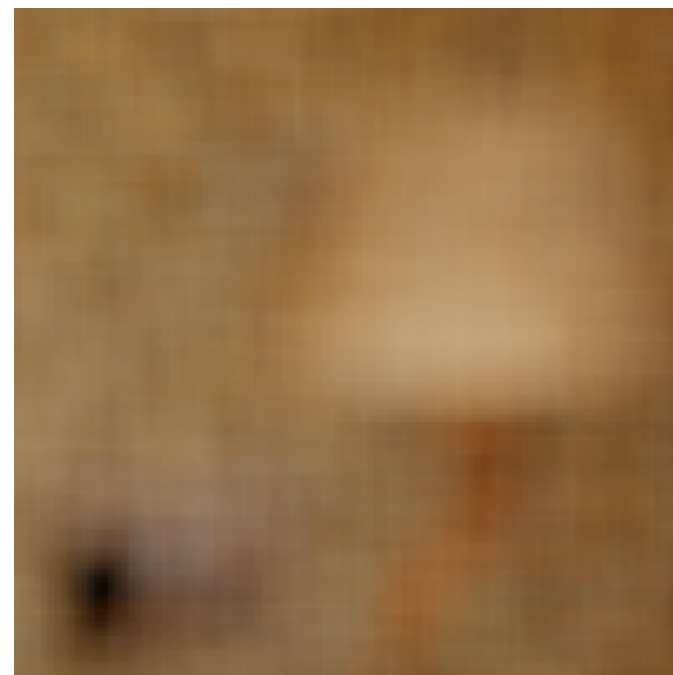
General:  $\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$

Box:  $\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p)^2$

Input – 256 spp



Box Filter



Weights:

Order:

Uniform

zero

Reference





# Filtering Framework — NLM [Rousselle et al. 2012]

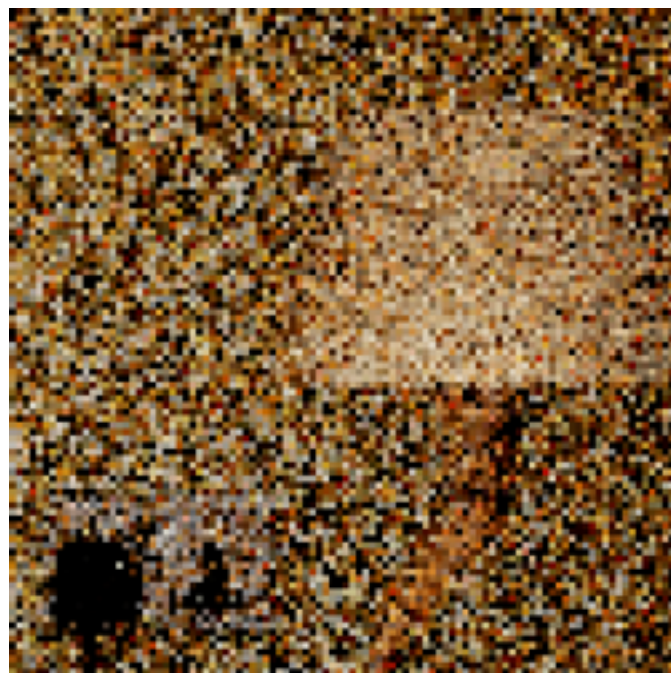
Based on the Non-Local Means filter of Buades et al. [2005]

$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

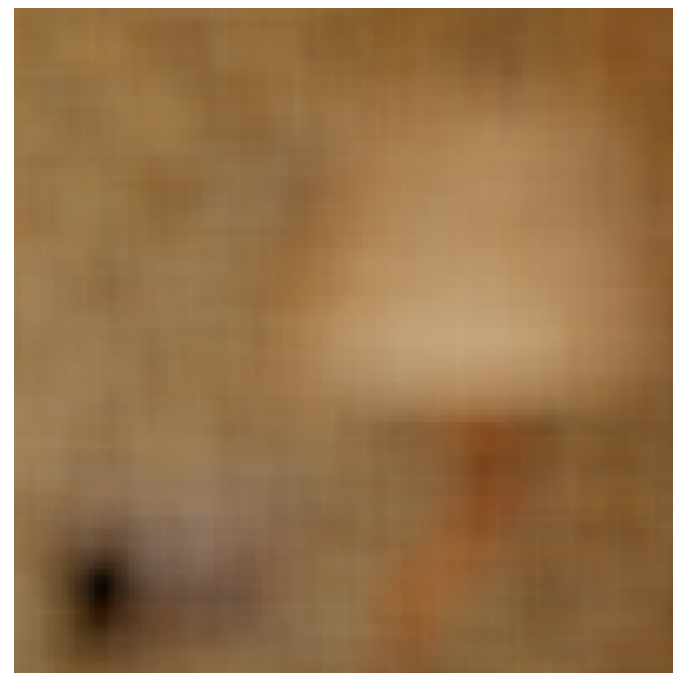
$$\text{NLM: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p)^2 \tilde{w}_{\mathbf{x}}(p, q)$$

$$\mathbf{x} = \{\text{Color}\}$$

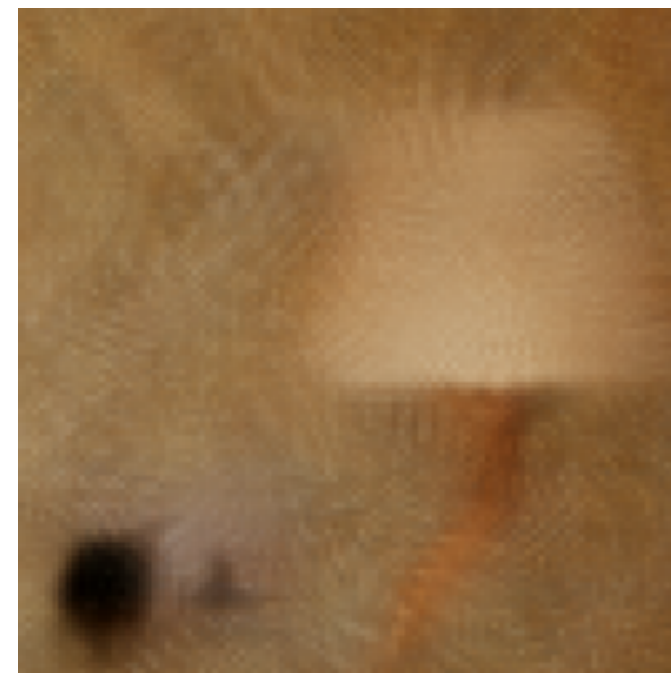
Input – 256 spp



Box Filter



NLM Filter



Reference



Weights:  
Order:

Uniform  
zero

NL-Means  
zero

# Filtering Framework — RDFC [Rousselle et al. 2013]

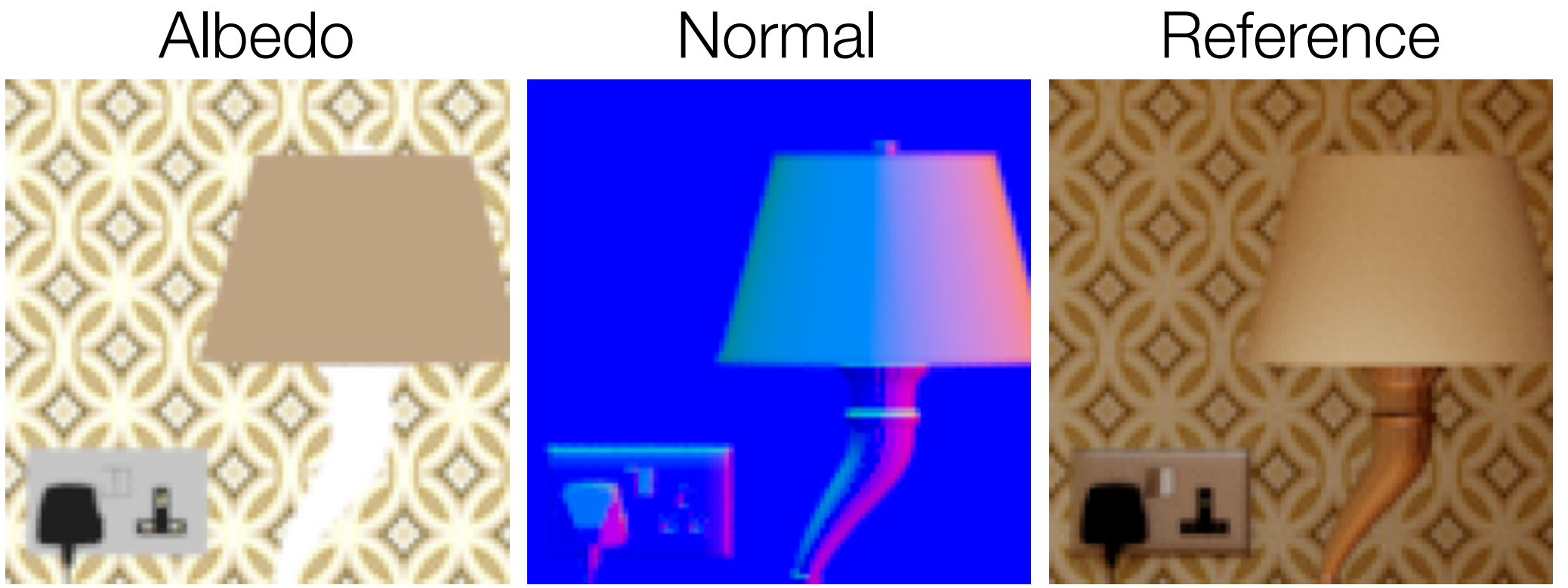
General:  $\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$

RDFC:  $\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p)^2 \tilde{w}_{\mathbf{x}}(p, q)$

$\mathbf{x} = \{\text{Color, Albedo, Normal, ...}\}$



Weights: Uniform, NL-Means  
Order: zero, zero





# Filtering Framework — RDFC [Rousselle et al. 2013]

$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

$$\text{RDFC: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p)^2 \tilde{w}_{\mathbf{x}}(p, q)$$

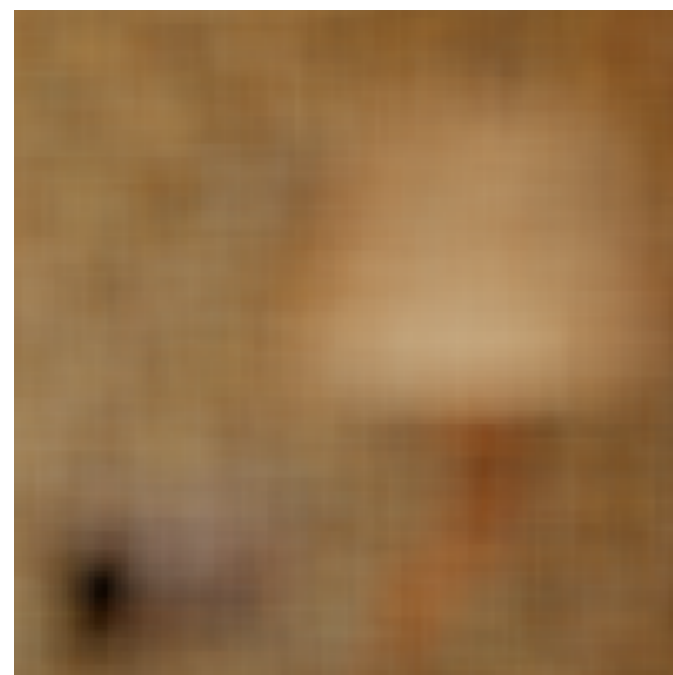
$\mathbf{x} = \{\text{Color, Albedo, Normal, ...}\}$

Input – 256 spp



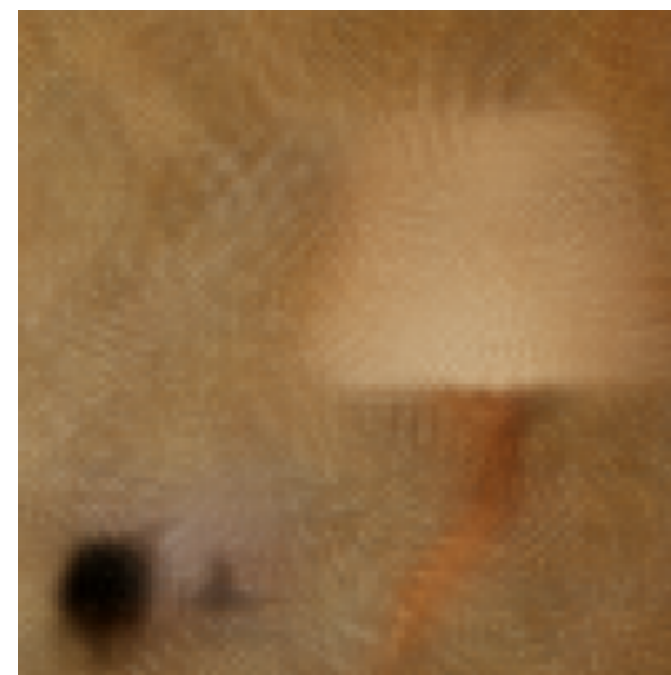
Weights:  
Order:

Box Filter



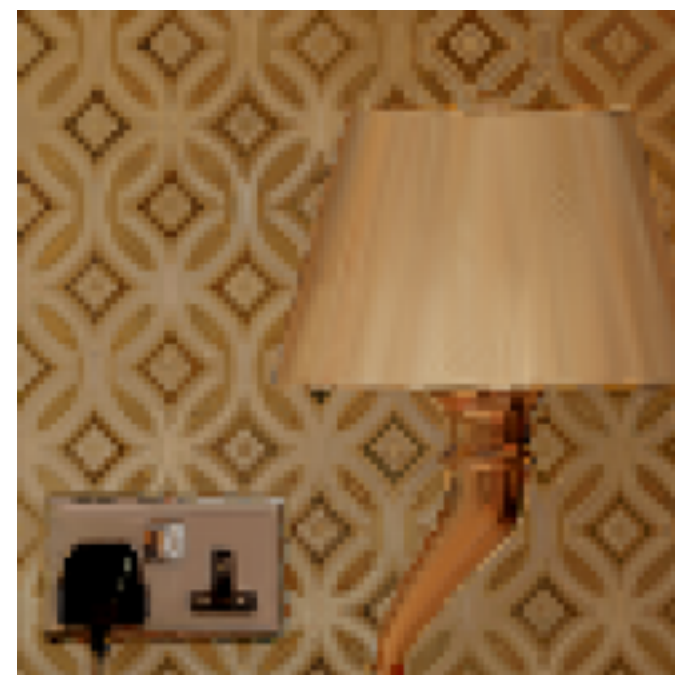
Uniform  
zero

NLM Filter



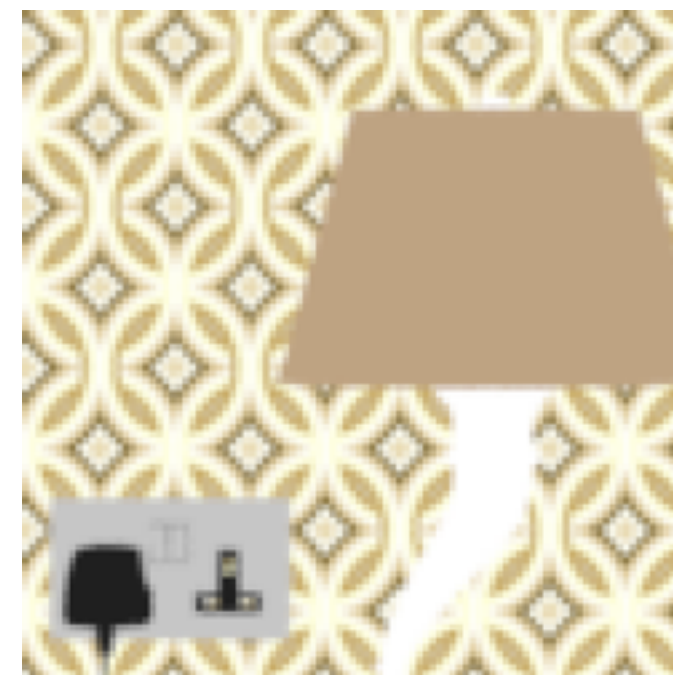
NL-Means  
zero

RDFC Filter



Joint NL-Means  
zero

Albedo



Normal



Reference





# Filtering Framework — RDFC [Rousselle et al. 2013]

$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

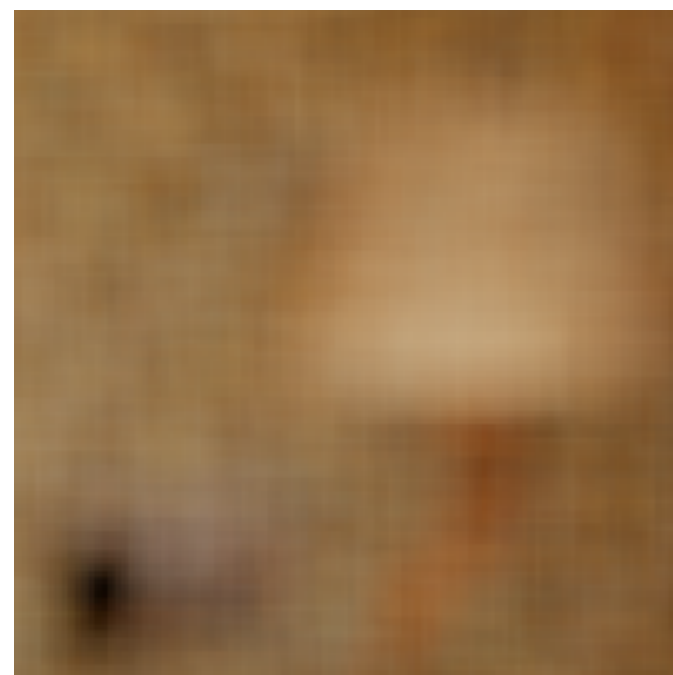
$$\text{RDFC: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p)^2 \tilde{w}_{\mathbf{x}}(p, q)$$

$\mathbf{x} = \{\text{Color, Albedo, Normal, ...}\}$

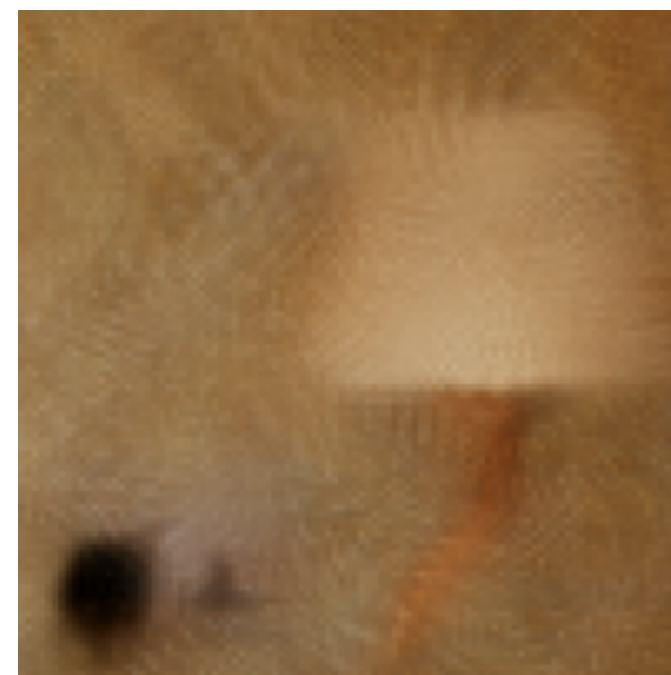
Input – 256 spp



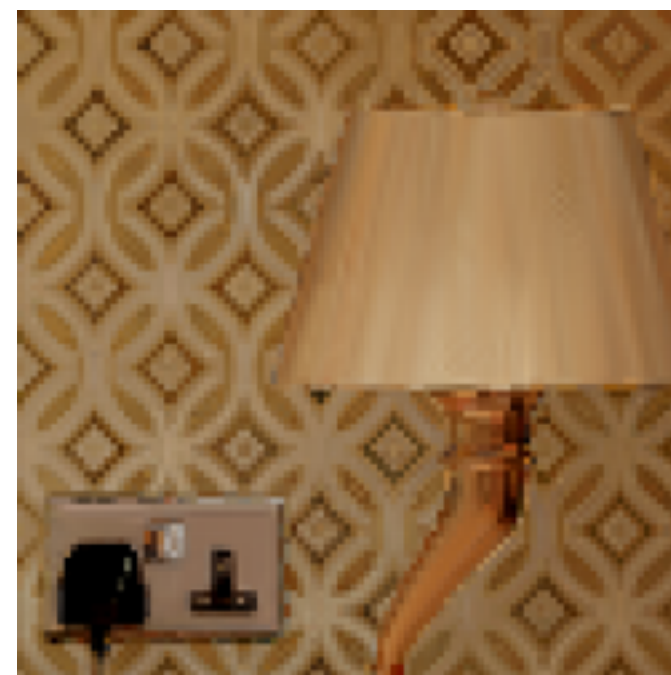
Box Filter



NLM Filter



RDFC Filter



Reference



Weights:  
Order:

Uniform  
zero

NL-Means  
zero

Joint NL-Means  
zero



# Filtering Framework — WLR [Moon et al. 2014]

$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

$$\text{WLR: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p - \nabla \hat{c}_p \cdot (\mathbf{x}_q - \mathbf{x}_p))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

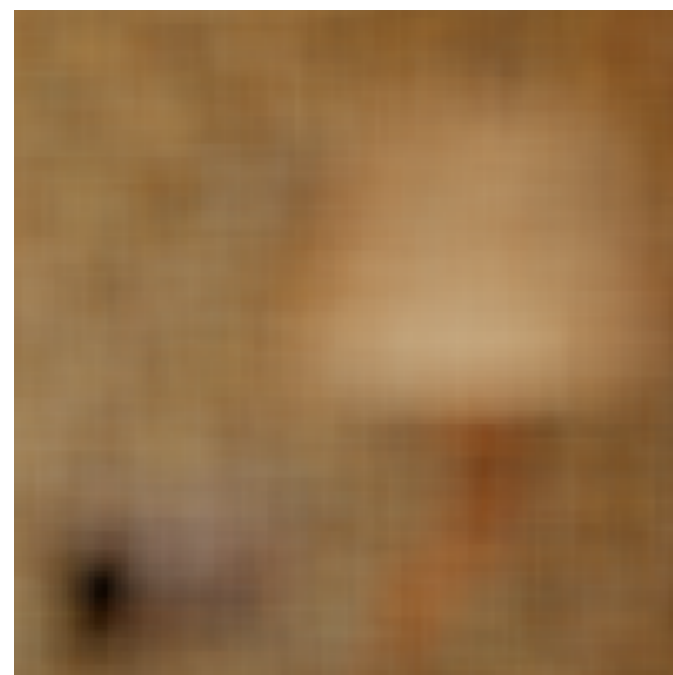
$\mathbf{x} = \{\text{Color, Albedo, Normal, ...}\}$

Input – 256 spp



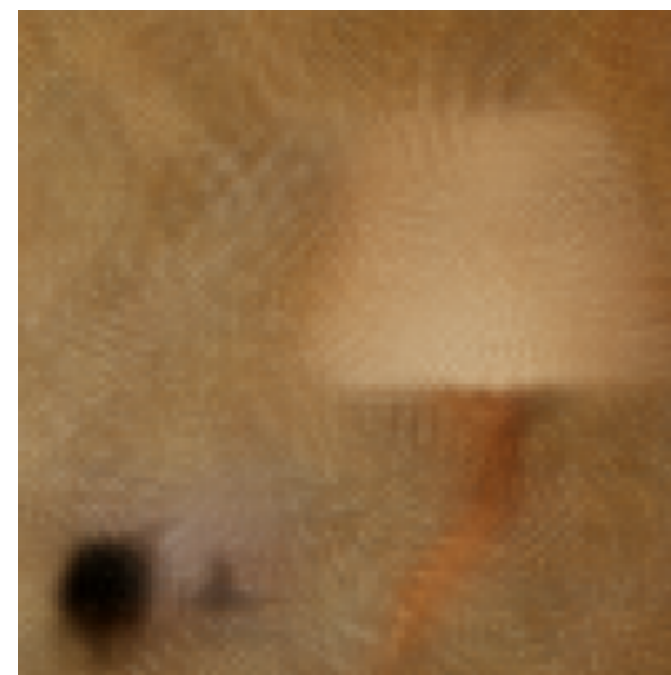
Weights:  
Order:

Box Filter



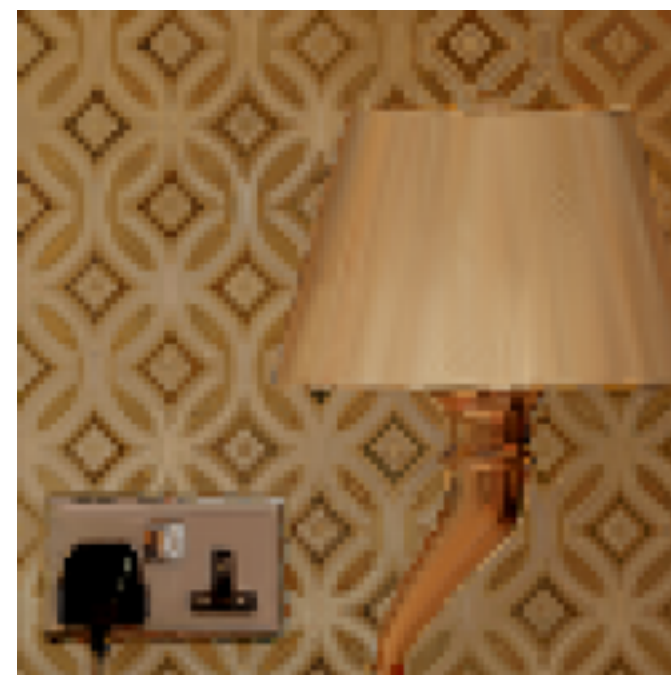
Uniform  
zero

NLM Filter



NL-Means  
zero

RDFC Filter



Joint NL-Means  
zero

WLR Filter



Cross-bilateral  
first

Reference





# Filtering Framework — WLR [Moon et al. 2014]

$$\text{General: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

$$\text{WLR: Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p - \nabla \hat{c}_p \cdot (\mathbf{x}_q - \mathbf{x}_p))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

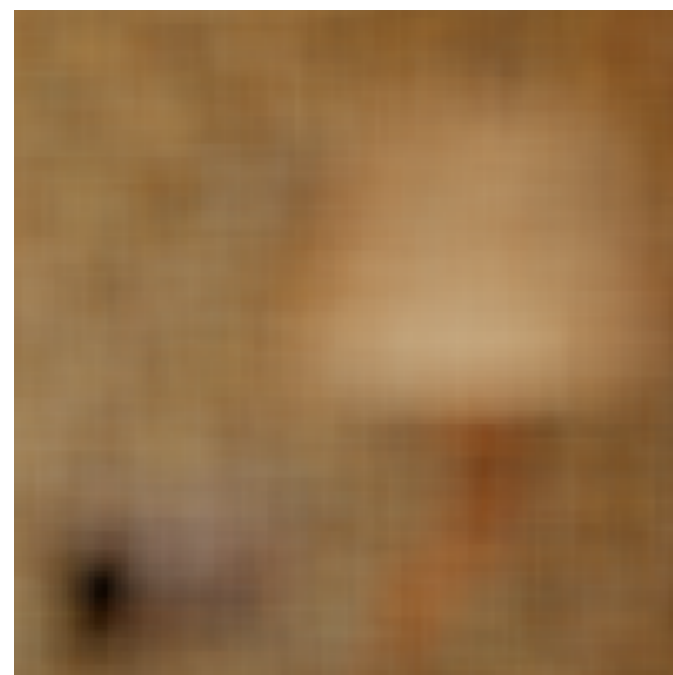
$\mathbf{x} = \{\text{Color, Albedo, Normal, ...}\}$

Input – 256 spp



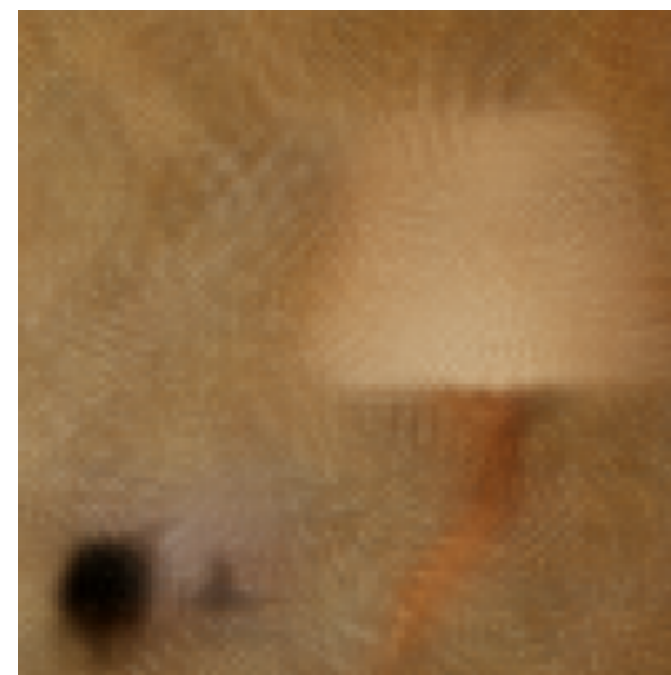
Weights:  
Order:

Box Filter



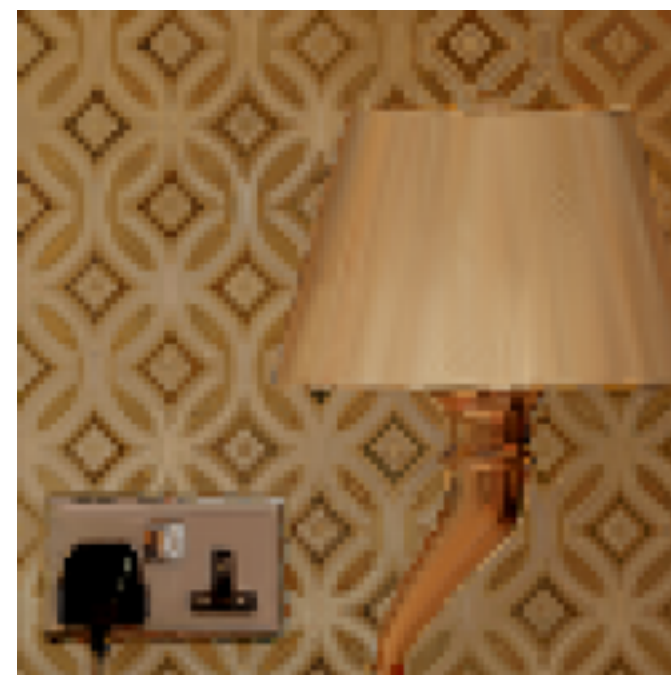
Uniform  
zero

NLM Filter



NL-Means  
zero

RDFC Filter



Joint NL-Means  
zero

WLR Filter



Cross-bilateral  
first

Reference





# Filtering Framework — Proposed Filter

General: 
$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

WLR: 
$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p - \nabla \hat{c}_p \cdot (\mathbf{x}_q - \mathbf{x}_p))^2 \tilde{w}_{\mathbf{y}}(p, q)$$

$\mathbf{x} = \{\text{Color, Albedo, Normal, ...}\}$

$\mathbf{y} = \{\text{Color}\}$



Weights:  
Order:

Uniform  
zero

NL-Means  
zero

Joint NL-Means  
zero

Cross-bilateral  
first

NL-Means  
first



# Filtering Framework — Proposed Filter

General: 
$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \tilde{m}_{\mathbf{x}}(p, q))^2 \tilde{w}_{\mathbf{x}}(p, q)$$

WLR: 
$$\text{Error}(\hat{c}_p) = \sum_{q \in \mathcal{N}_p} (c_q - \hat{c}_p - \nabla \hat{c}_p \cdot (\mathbf{x}_q - \mathbf{x}_p))^2 \tilde{w}_{\mathbf{y}}(p, q)$$

$\mathbf{x} = \{\text{Color, Albedo, Normal, ...}\}$        $\mathbf{y} = \{\text{Color}\}$



Weights:      Uniform      NL-Means      Joint NL-Means      Cross-bilateral      NL-Means  
 Order:      zero      zero      zero      first      first



# Algorithm Overview





# Algorithm Overview



# Algorithm Overview

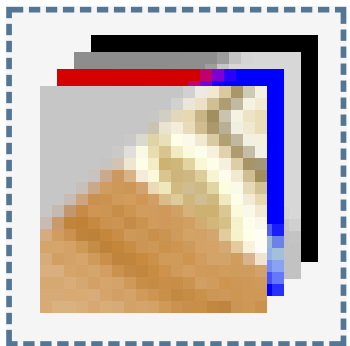
variance



noisy input



feature buffers

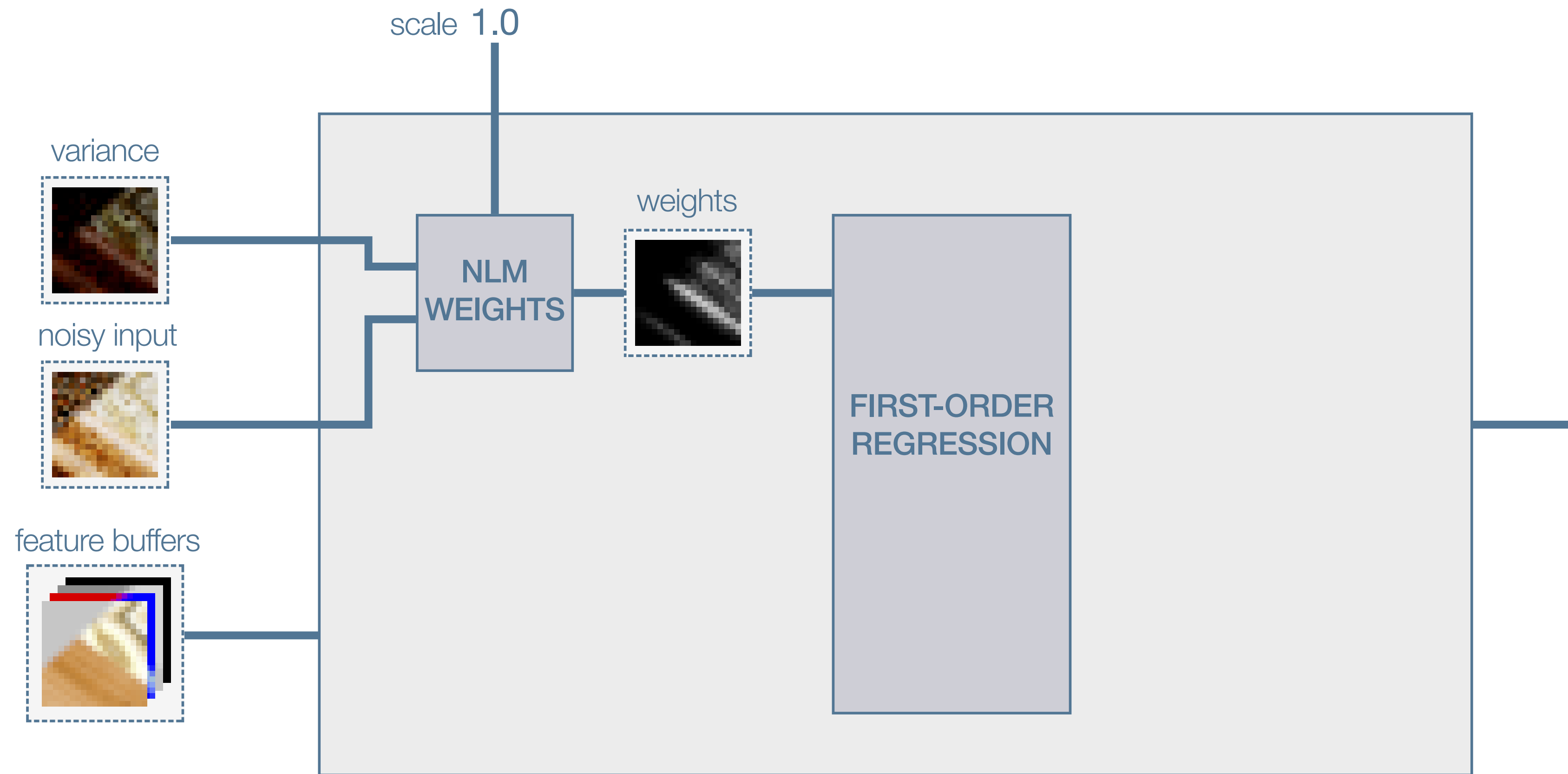




# Algorithm Overview

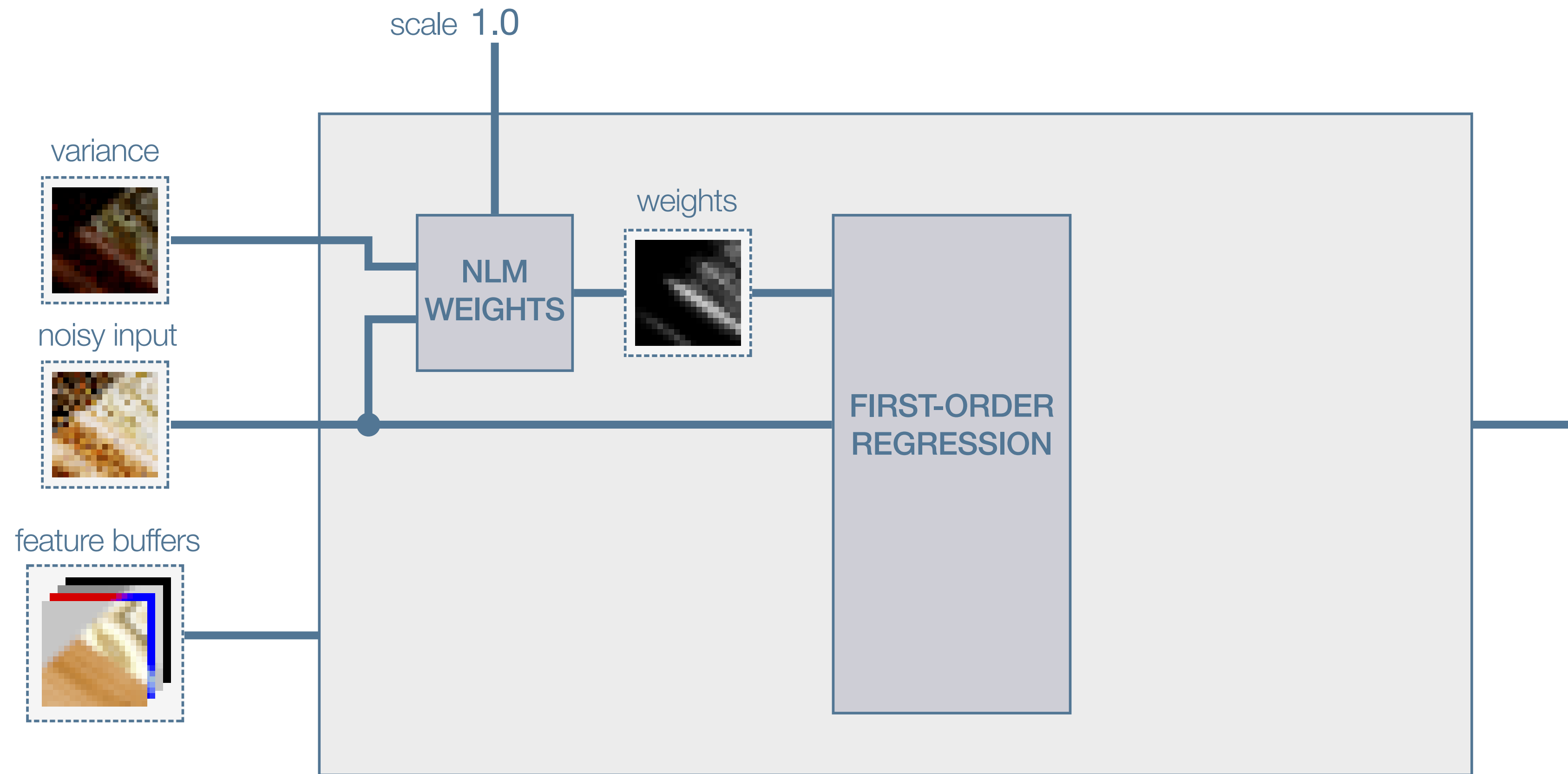


# Algorithm Overview

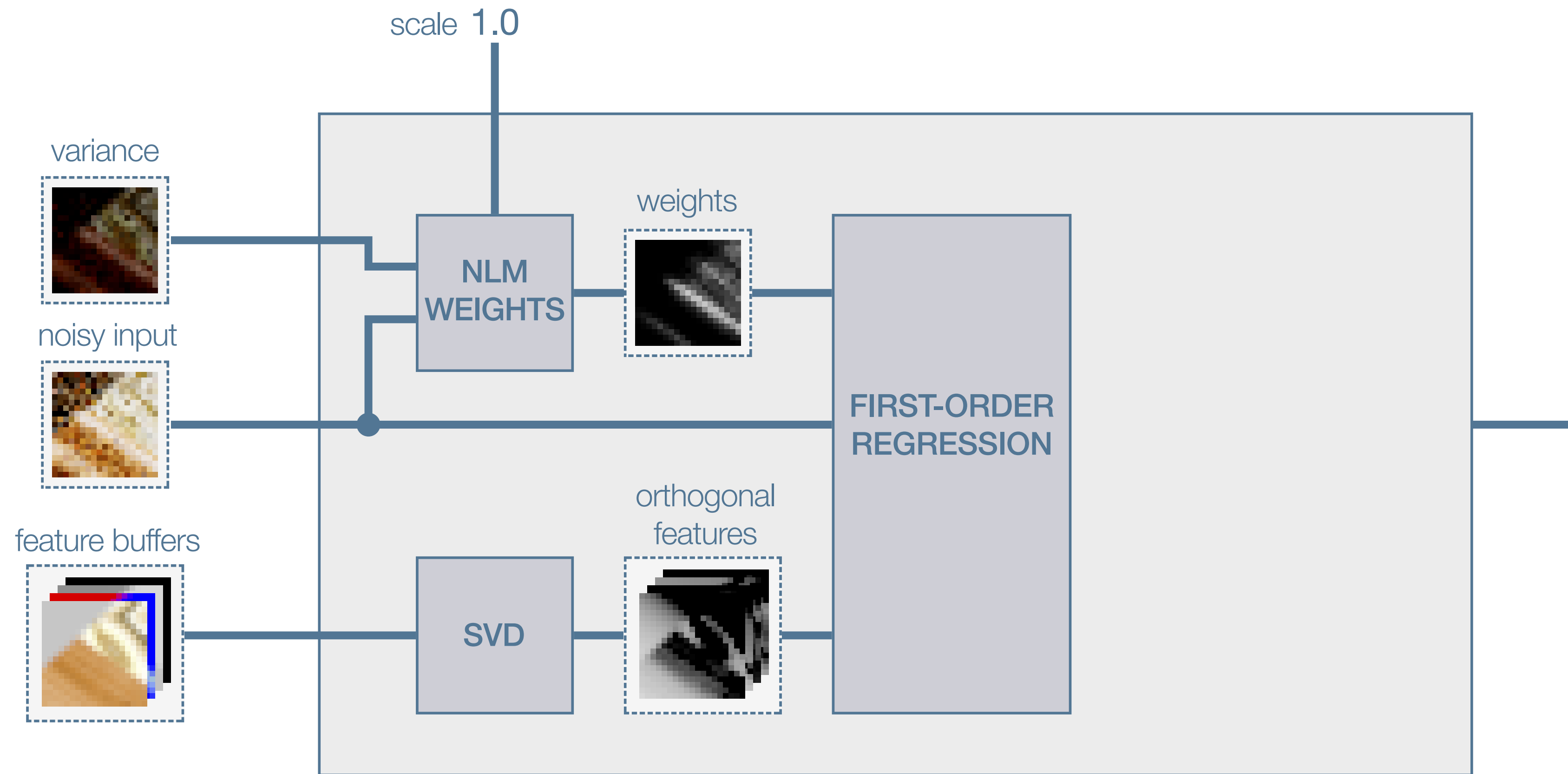




# Algorithm Overview

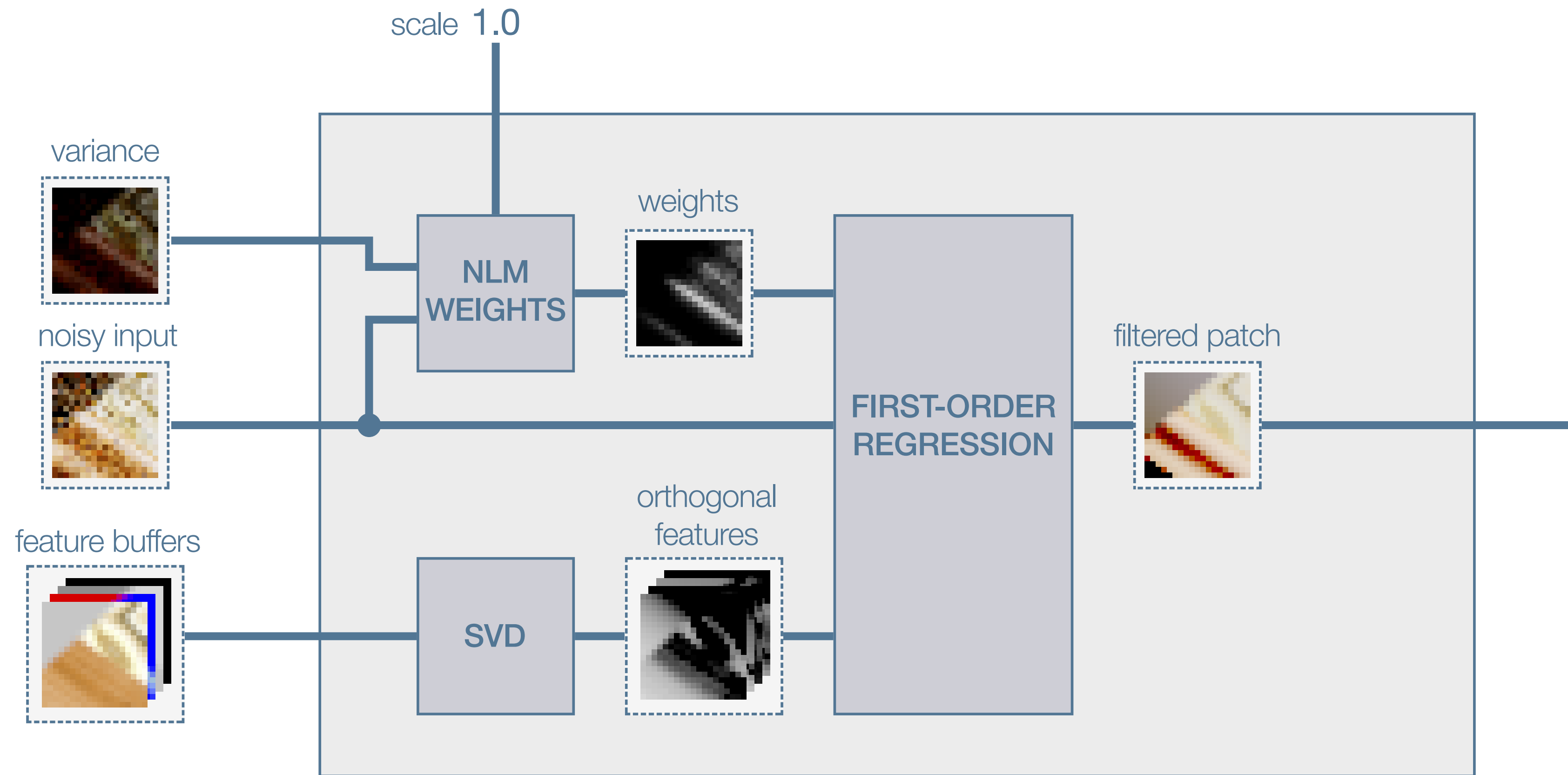


# Algorithm Overview

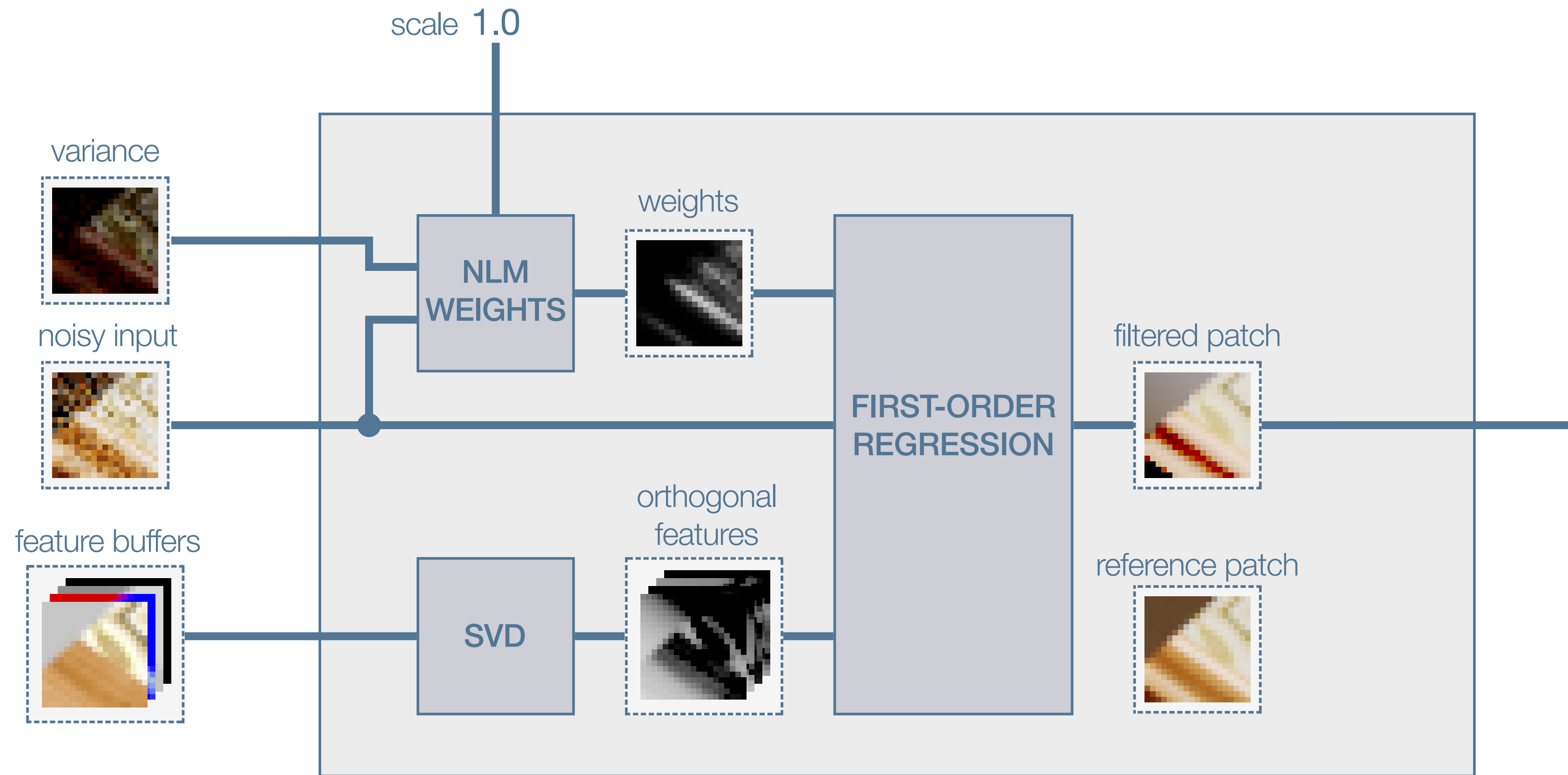




# Algorithm Overview

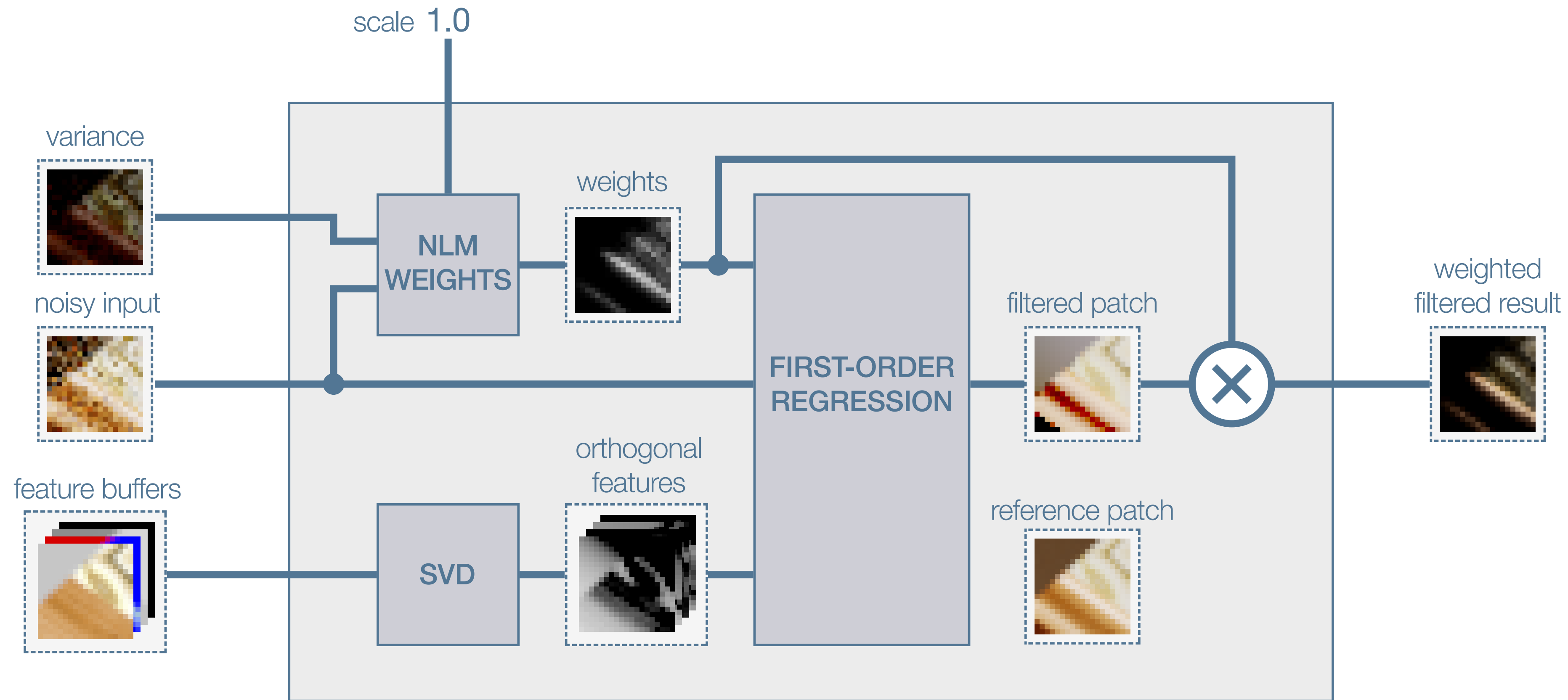


# Algorithm Overview

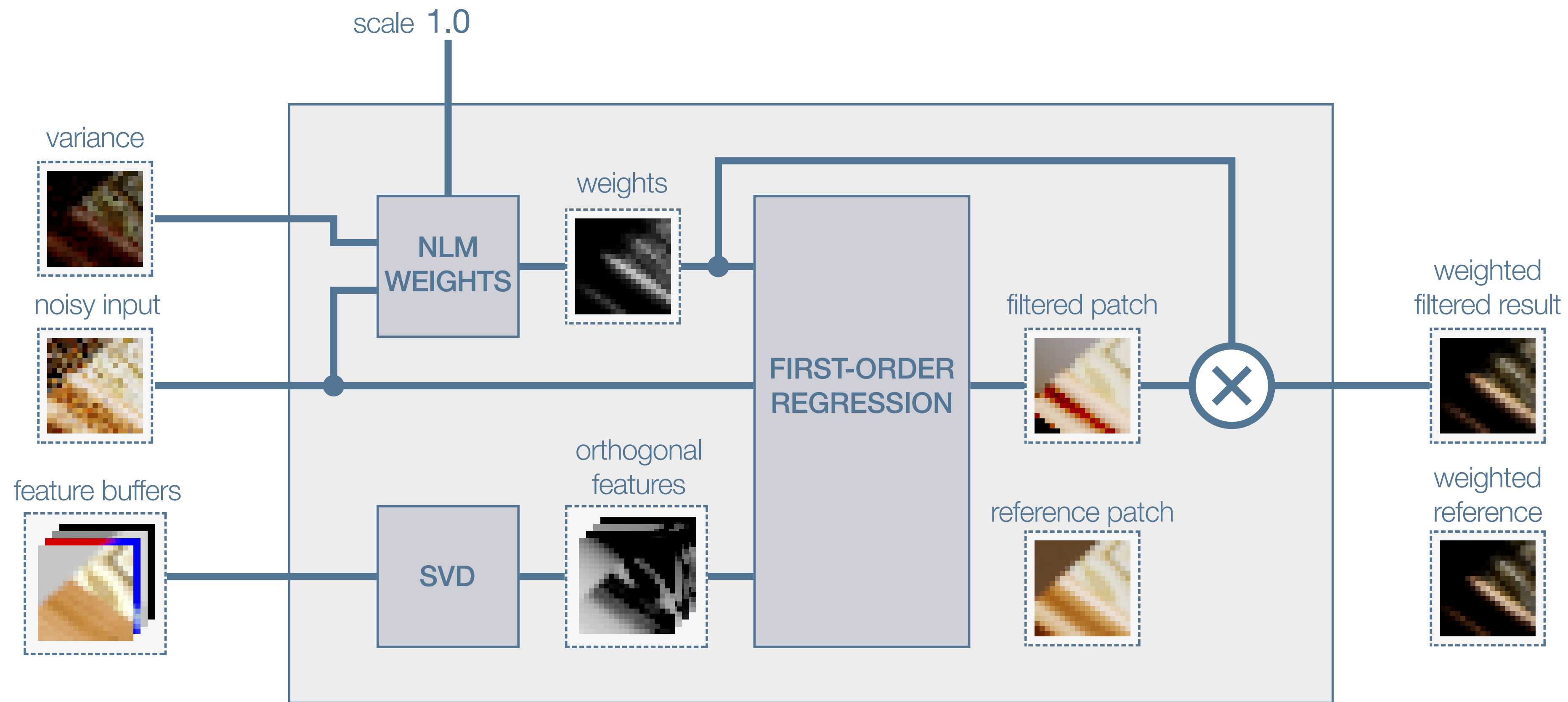




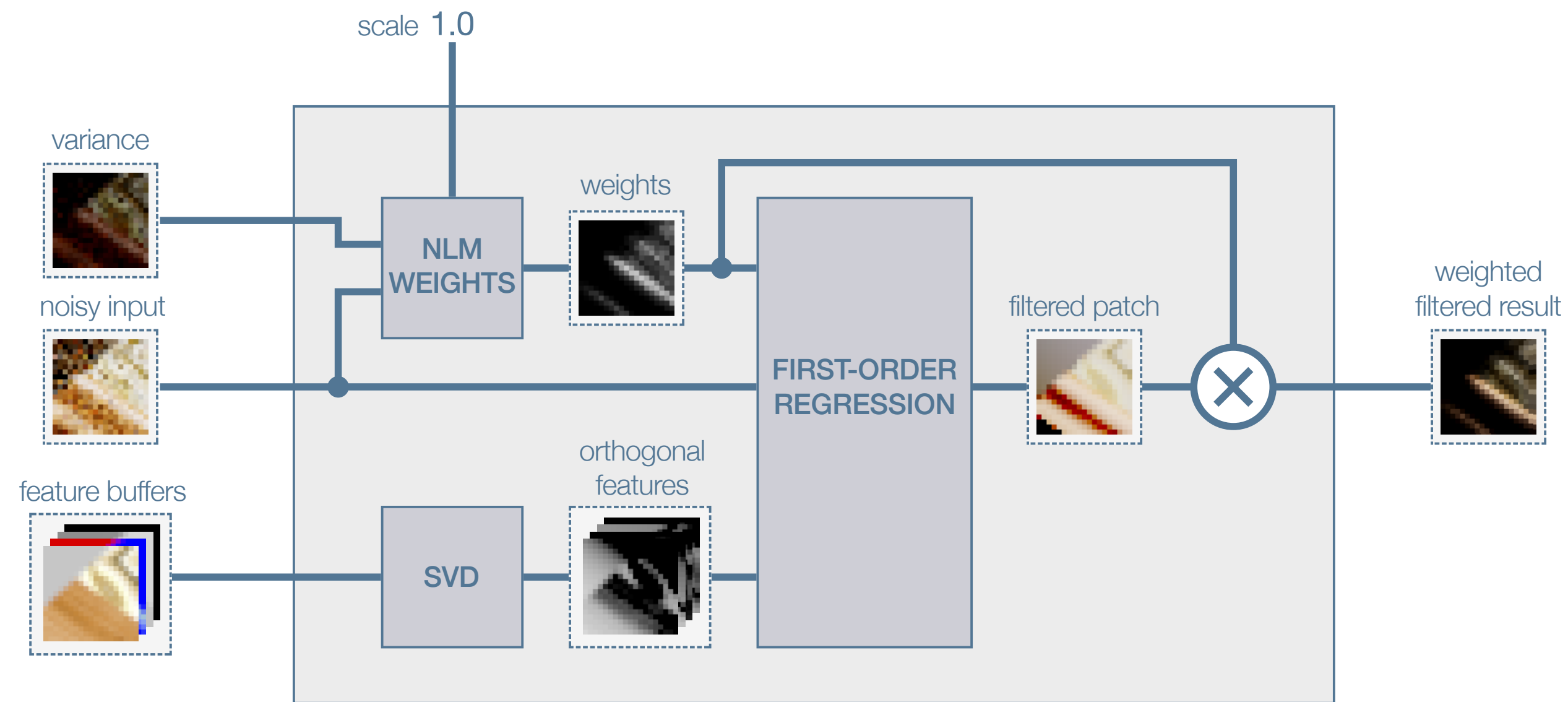
# Algorithm Overview



# Algorithm Overview

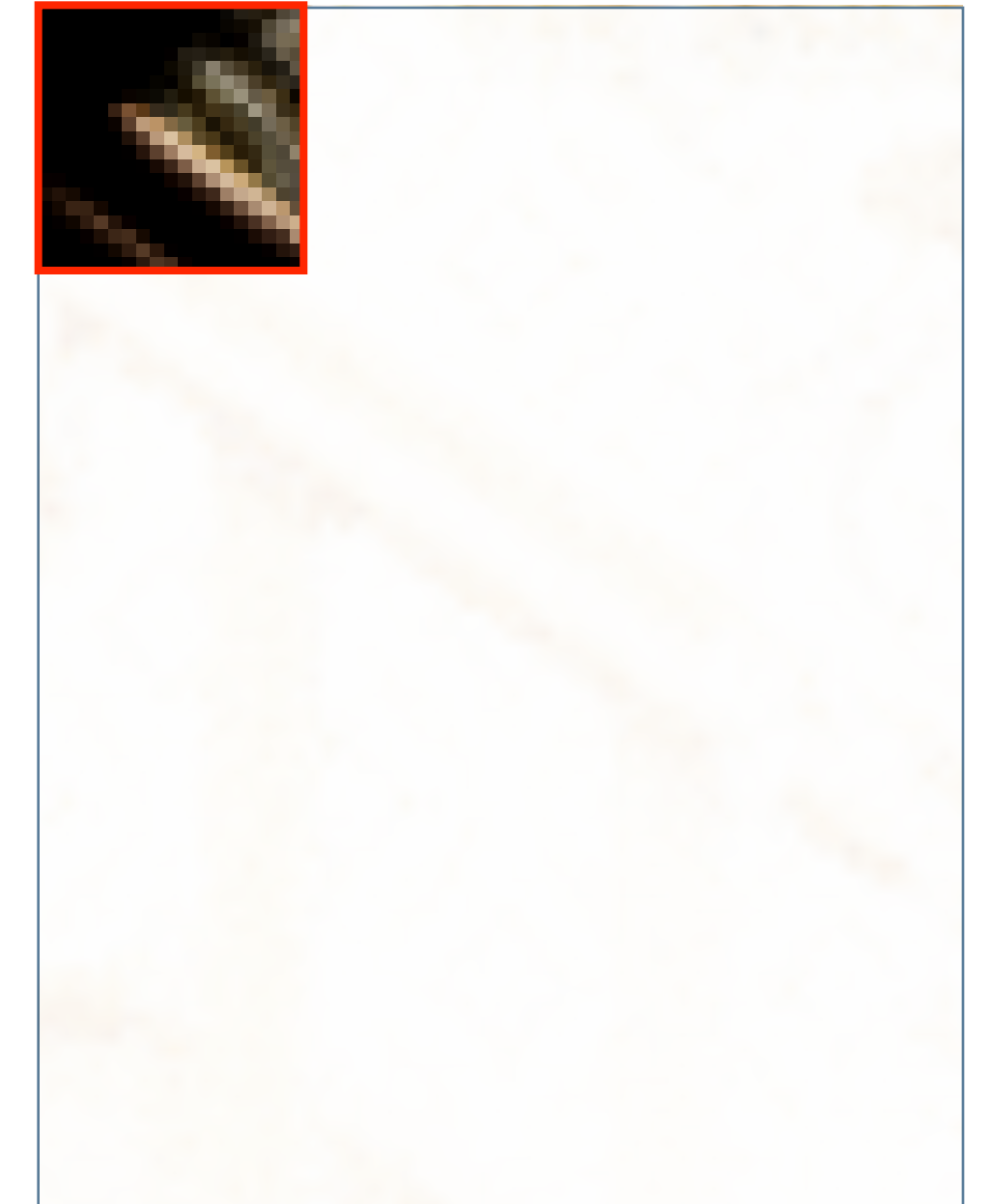
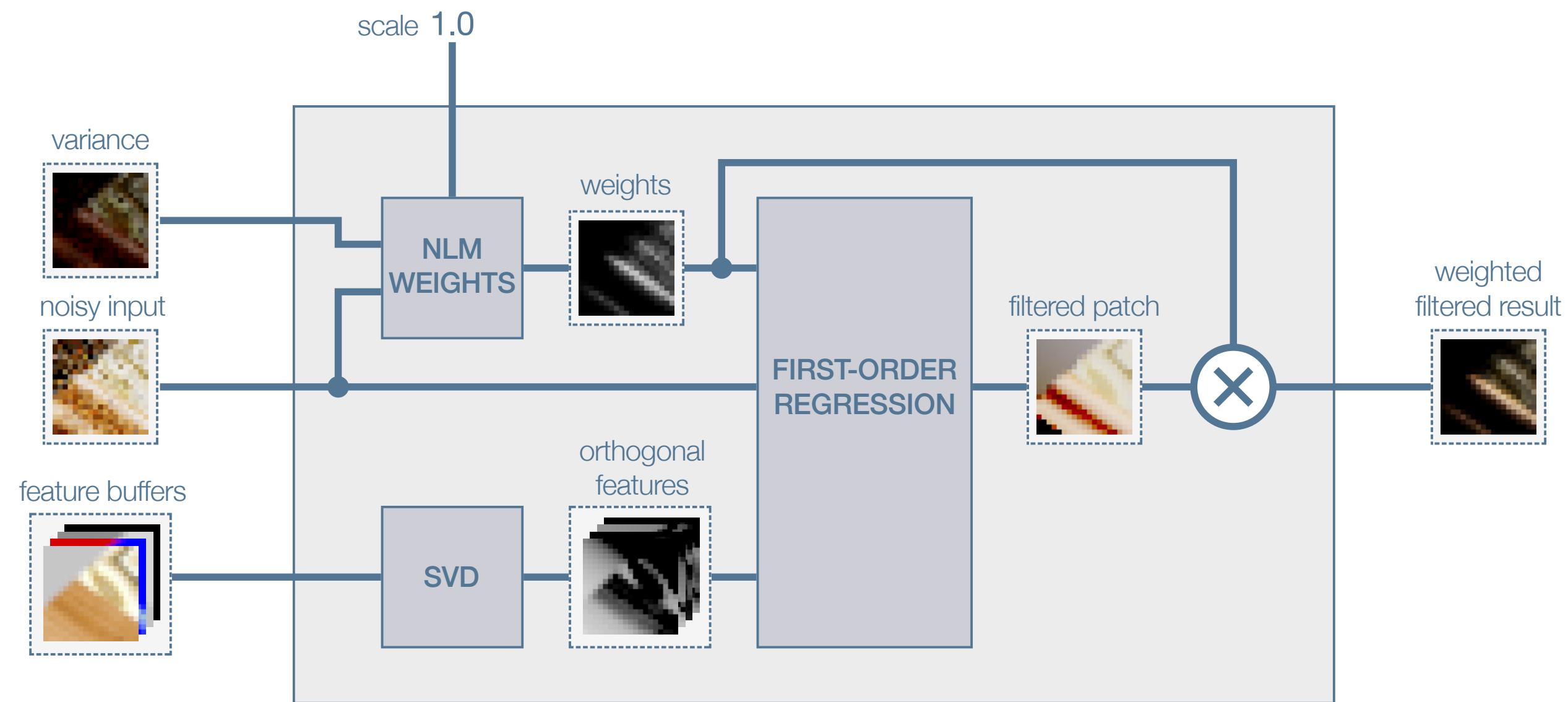


# Algorithm Overview

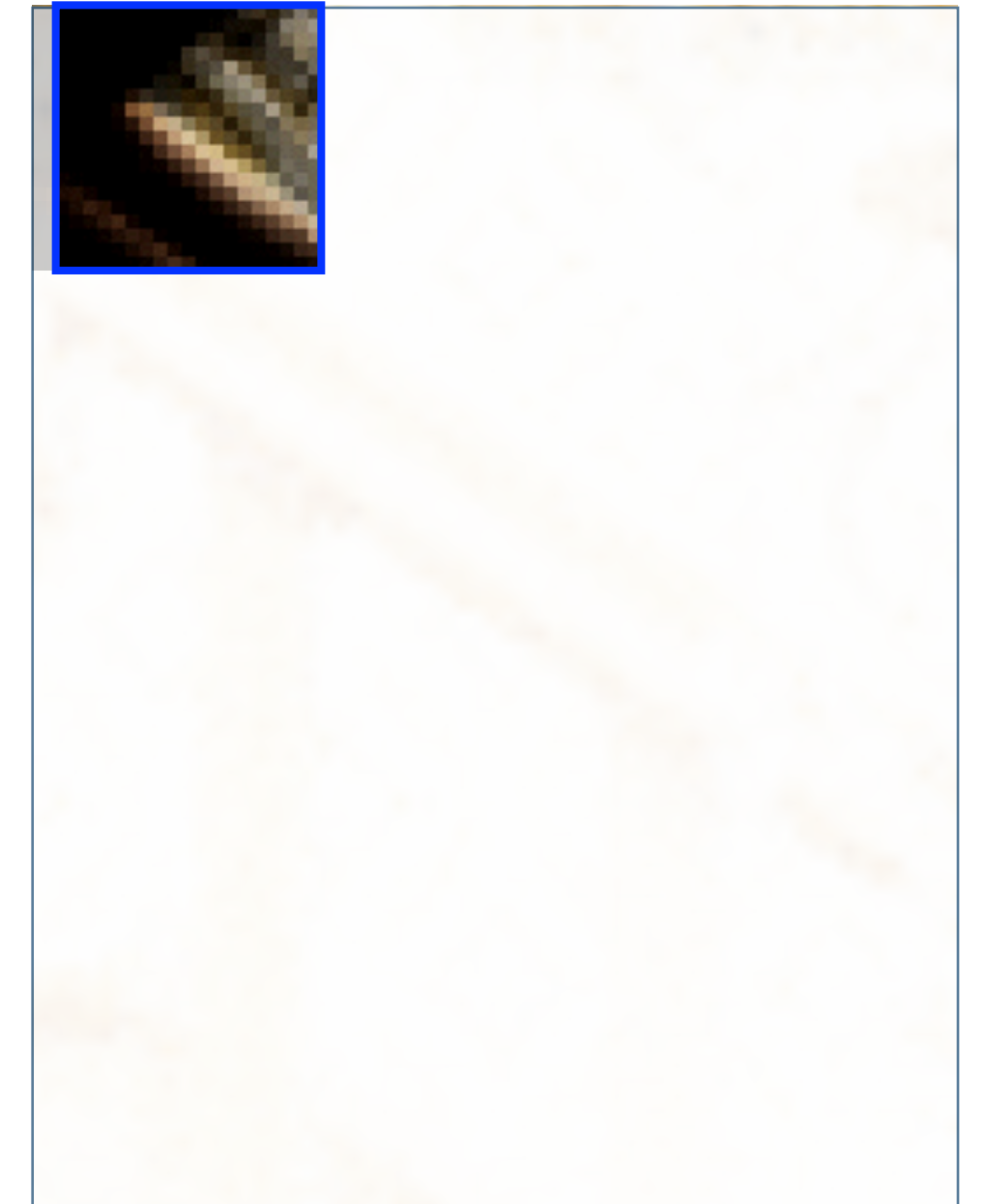
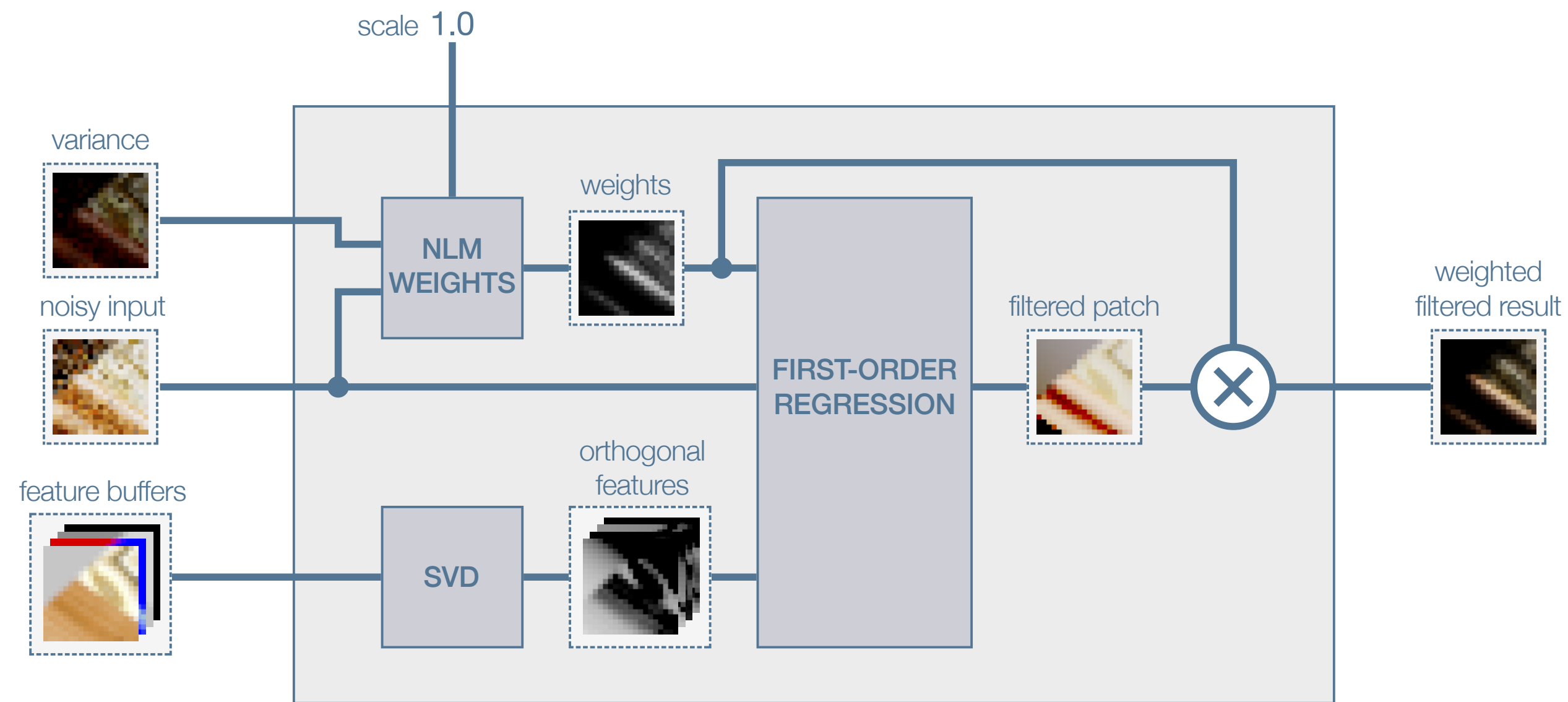




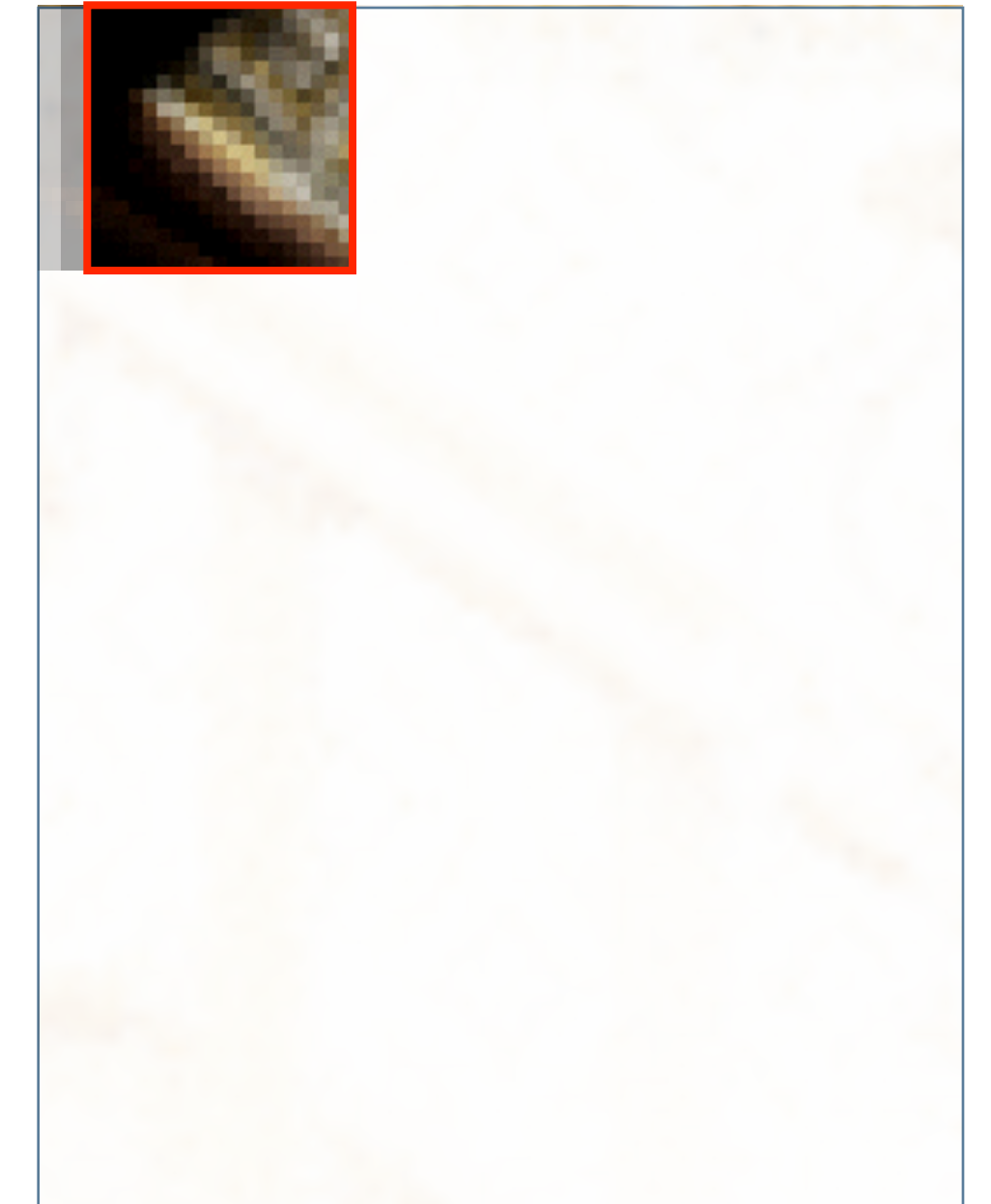
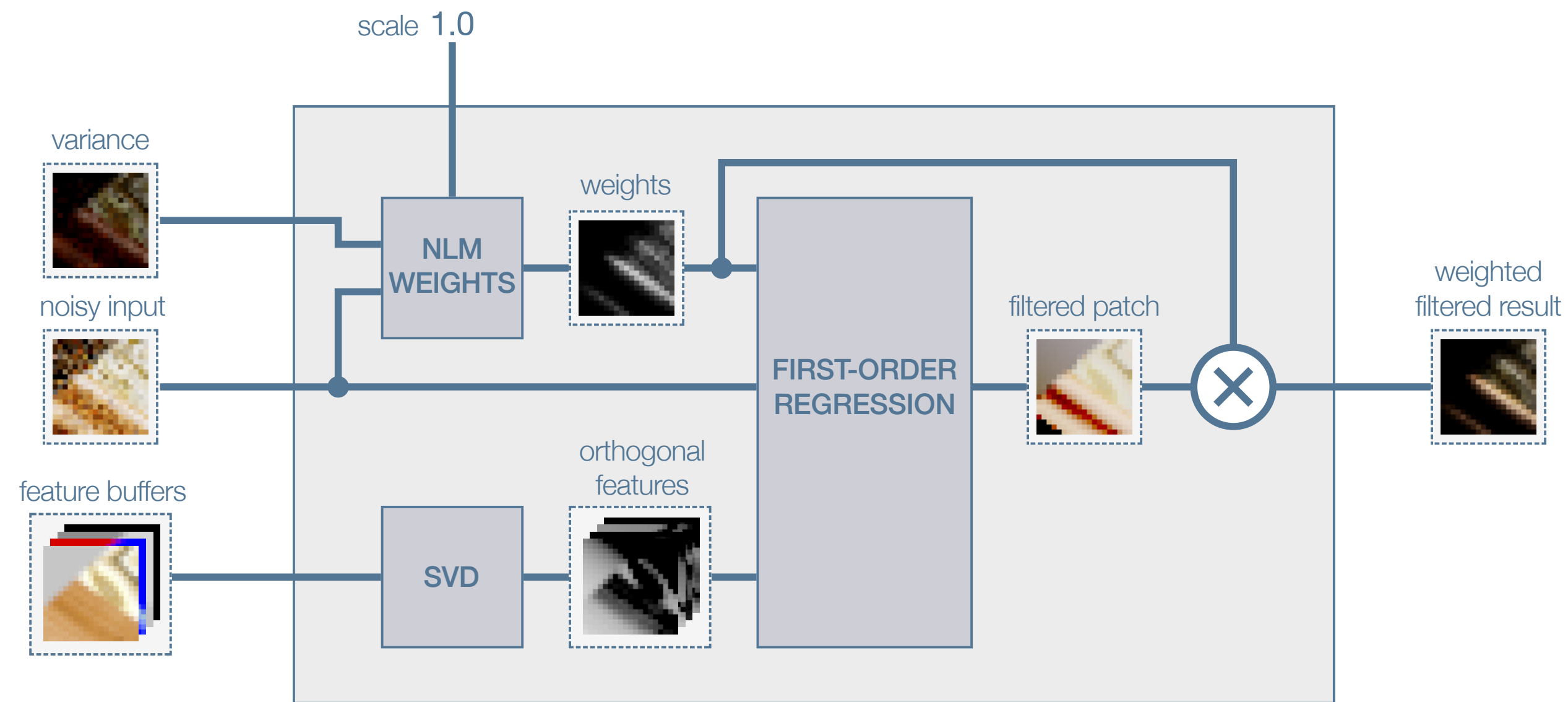
# Algorithm Overview



# Algorithm Overview

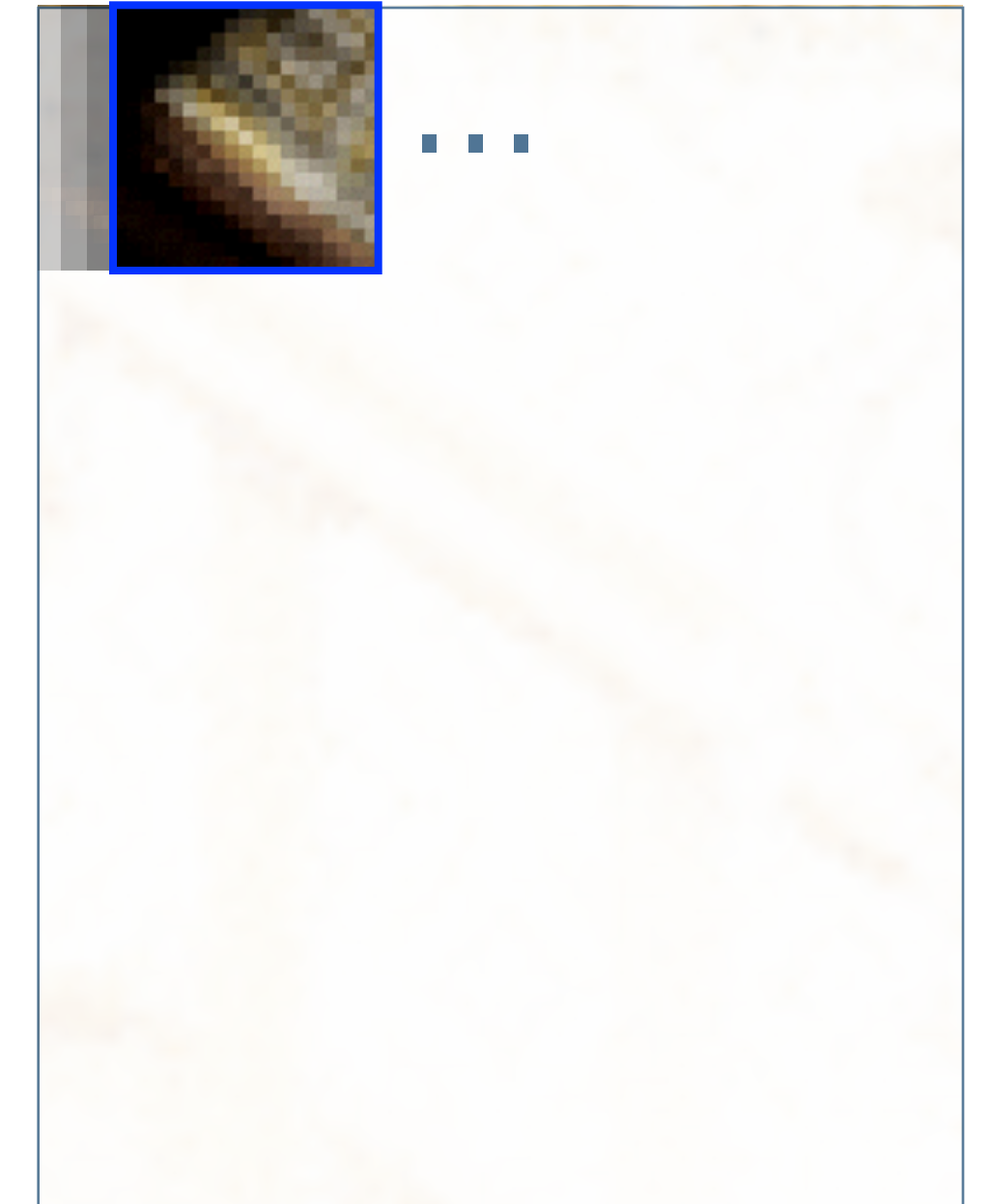
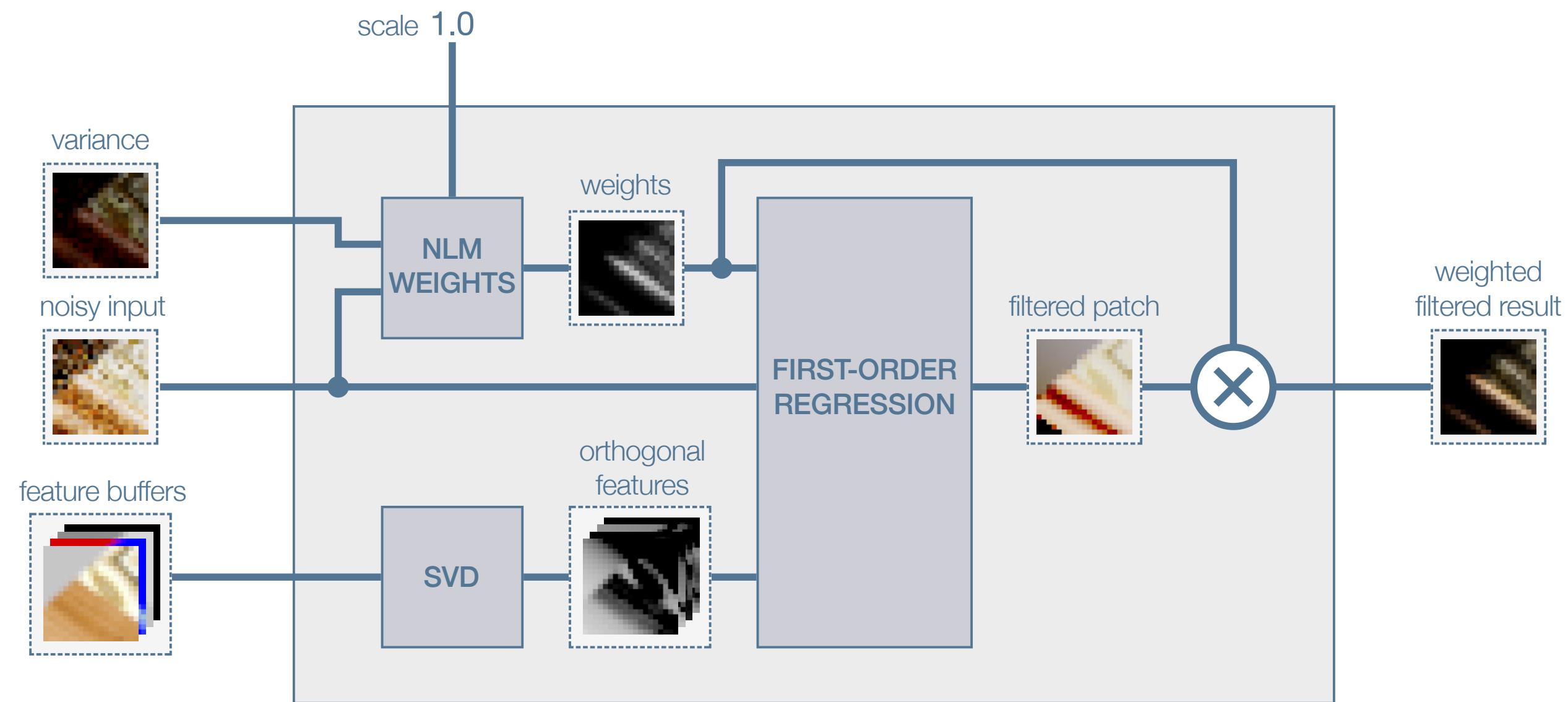


# Algorithm Overview

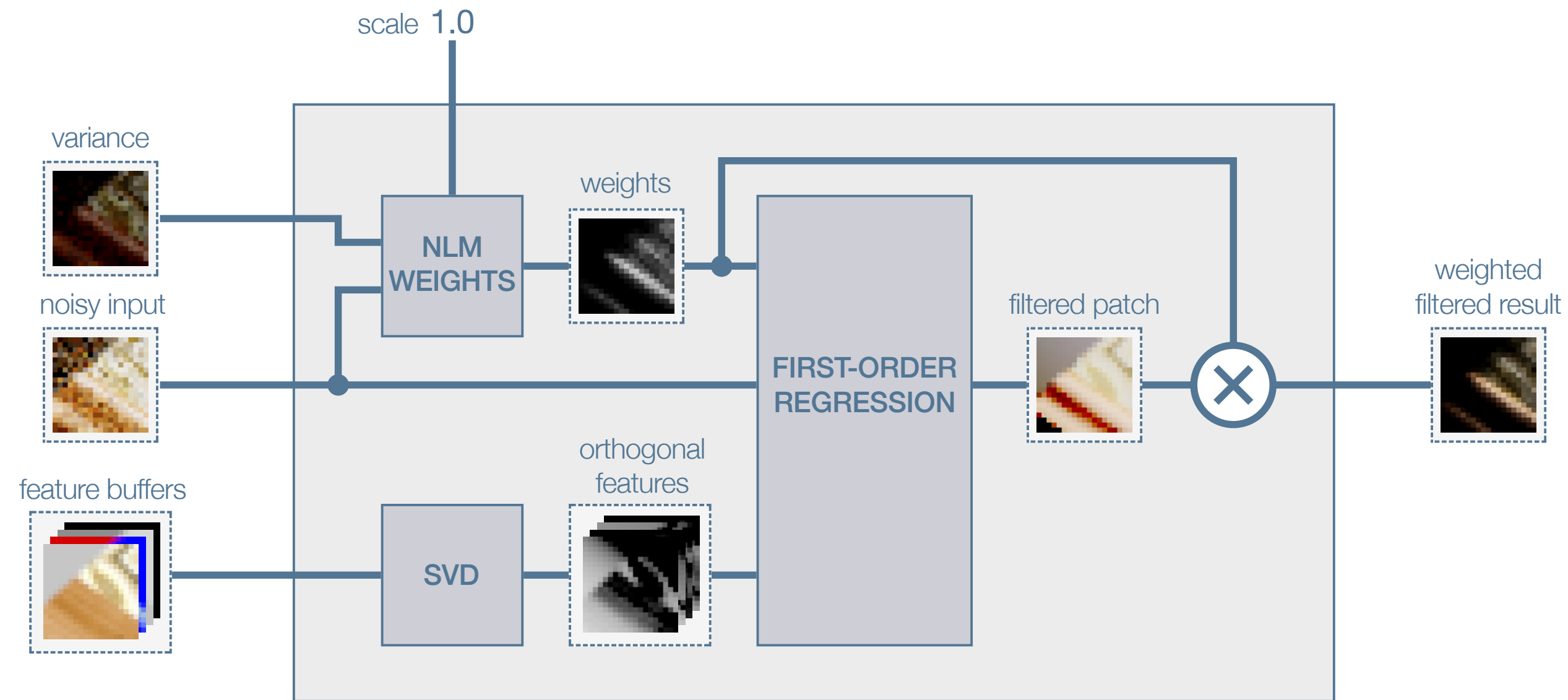




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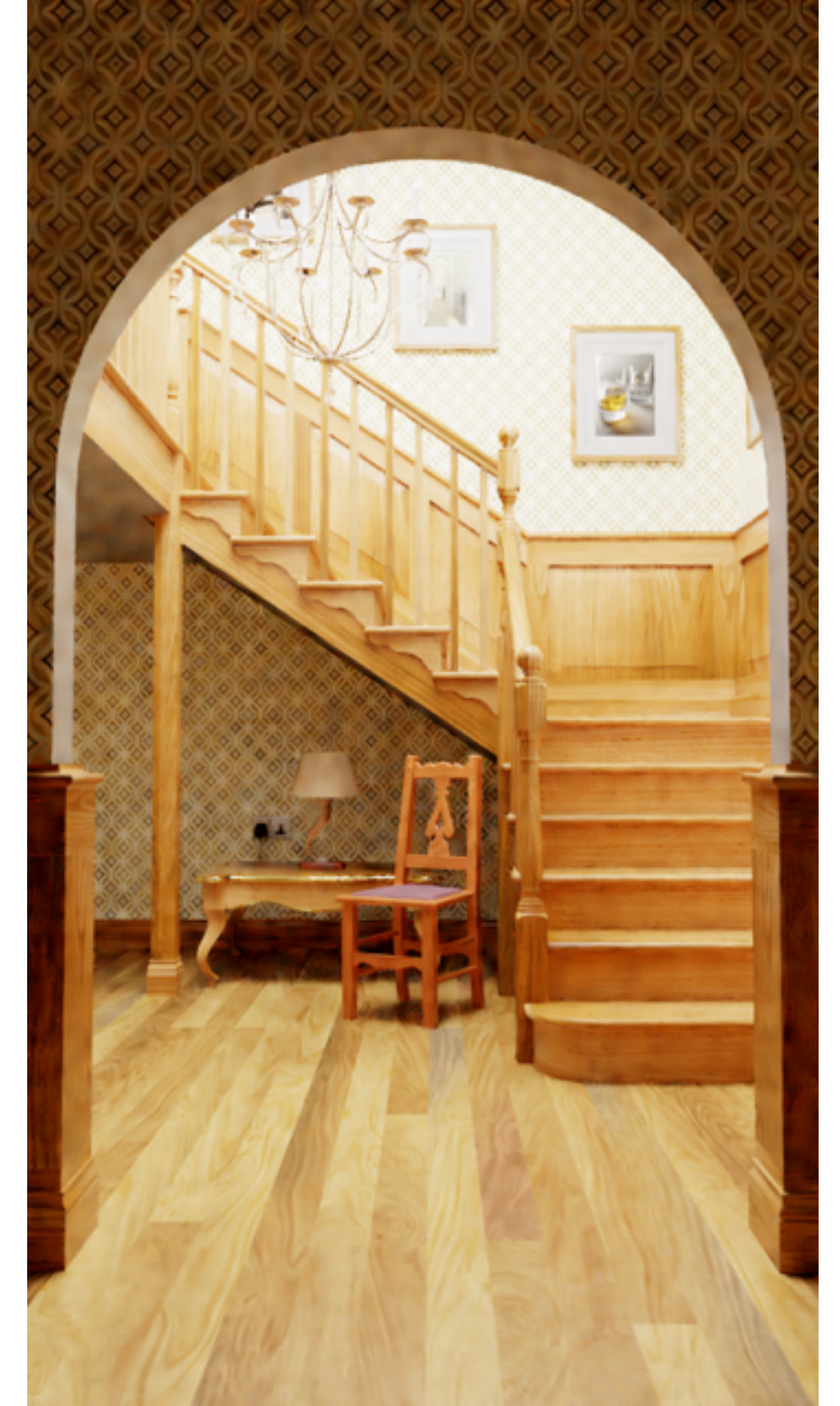
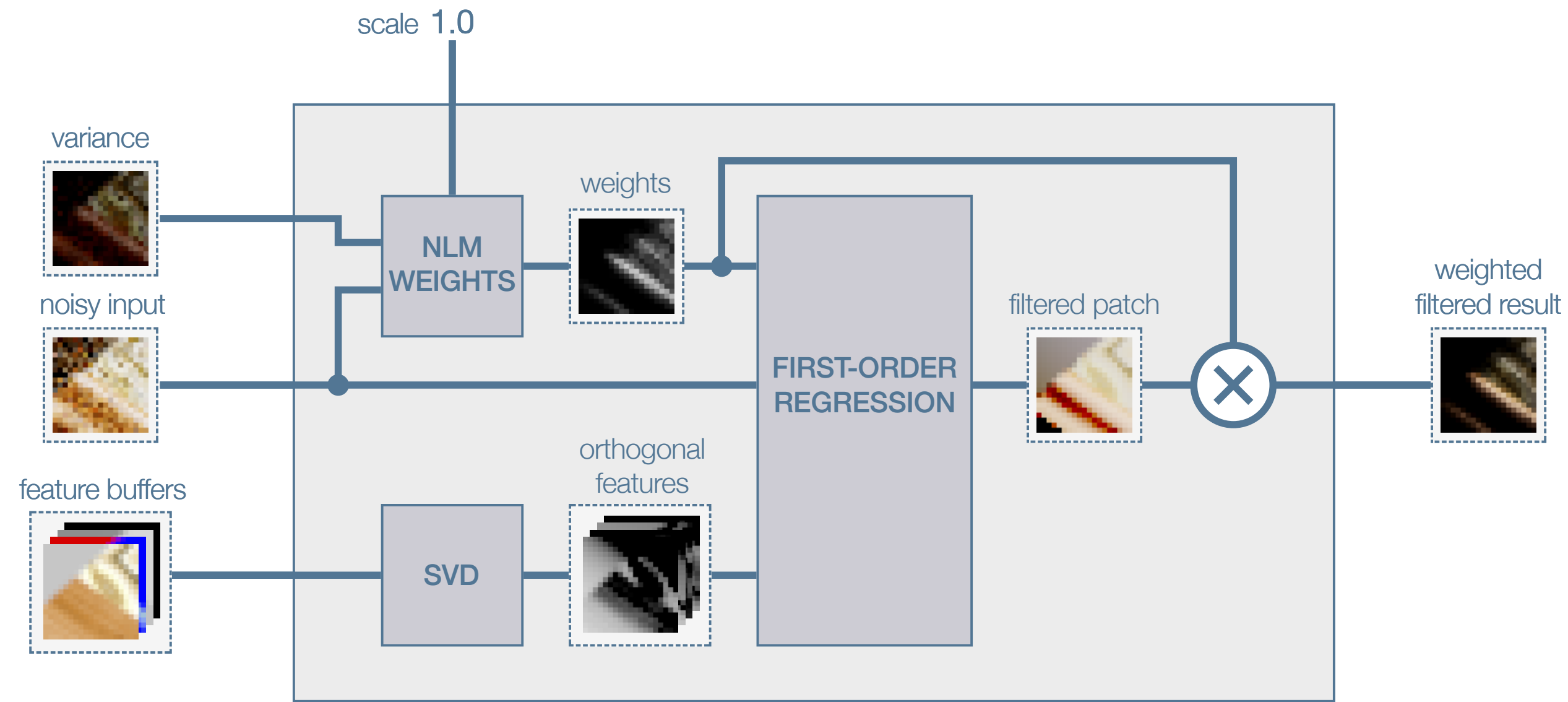


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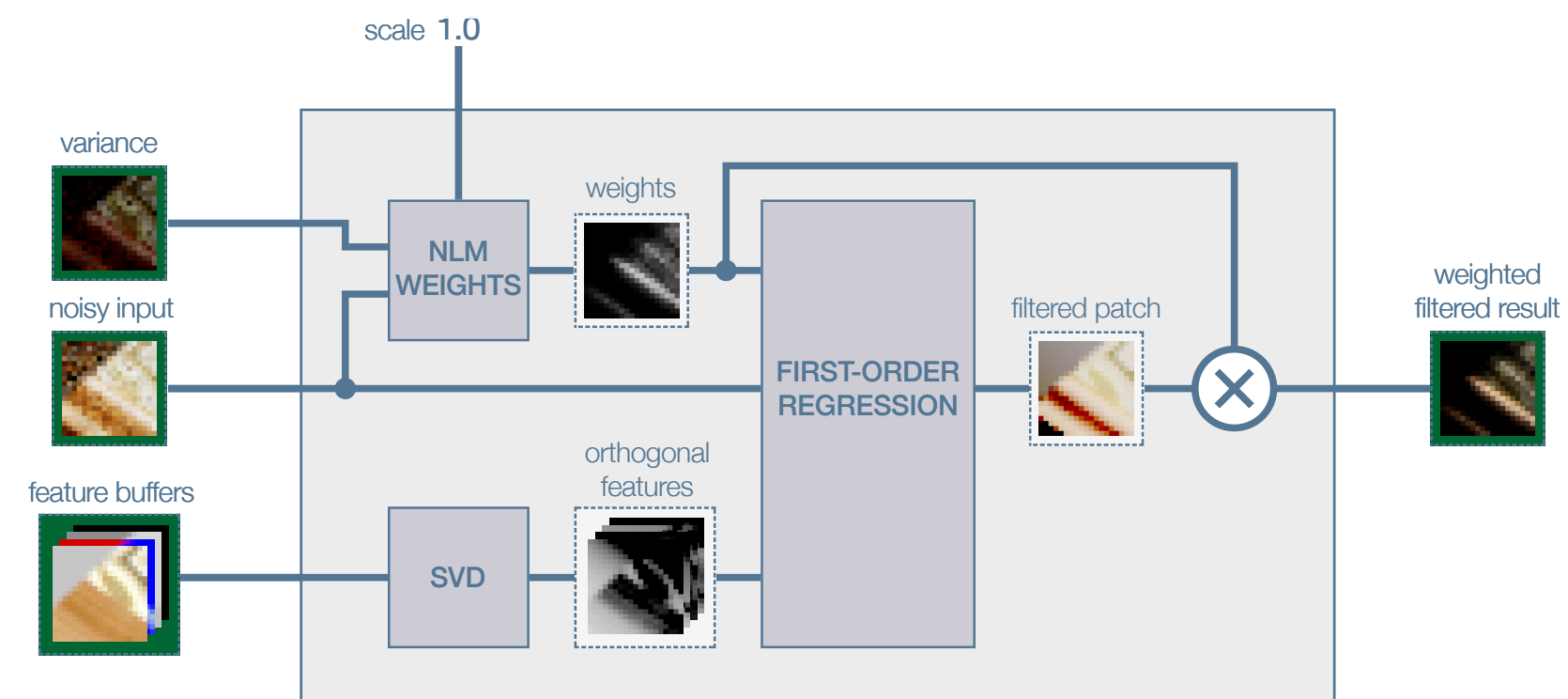
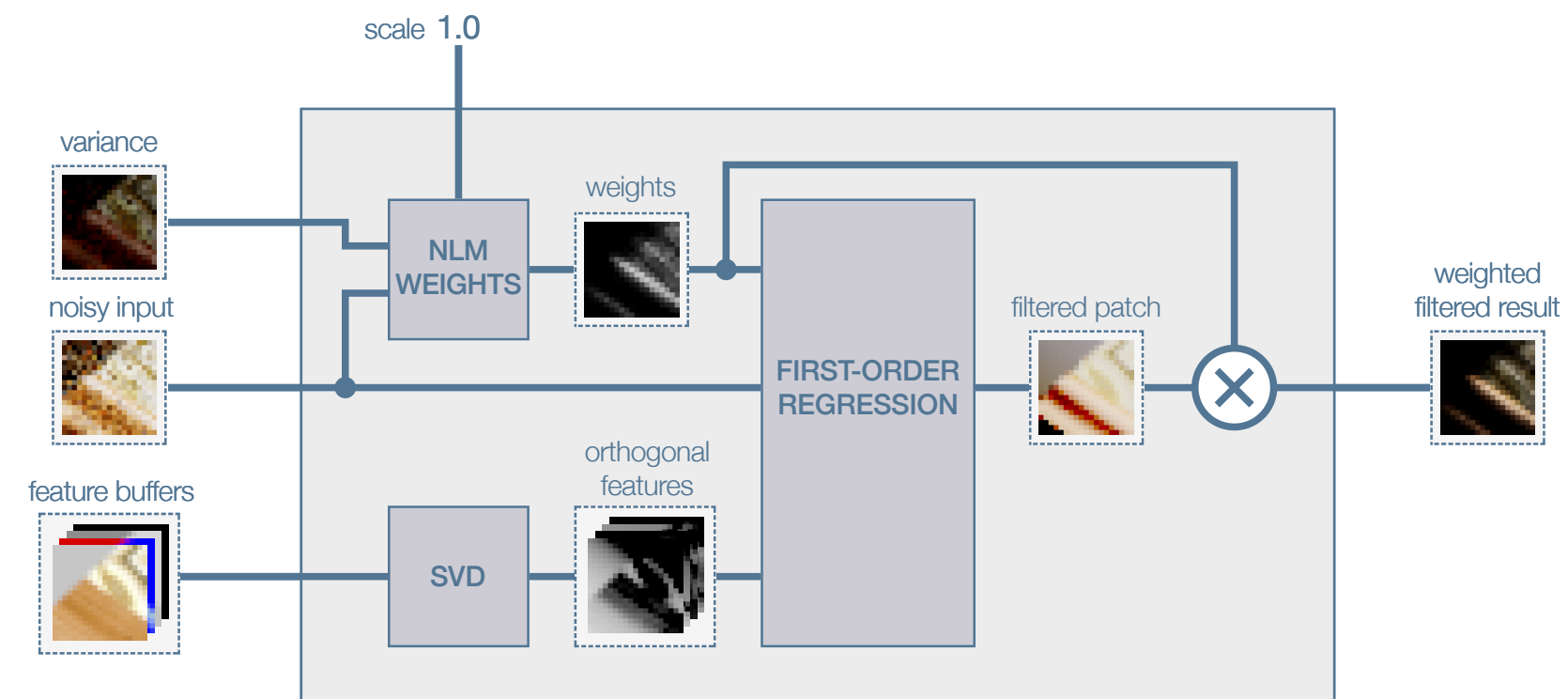


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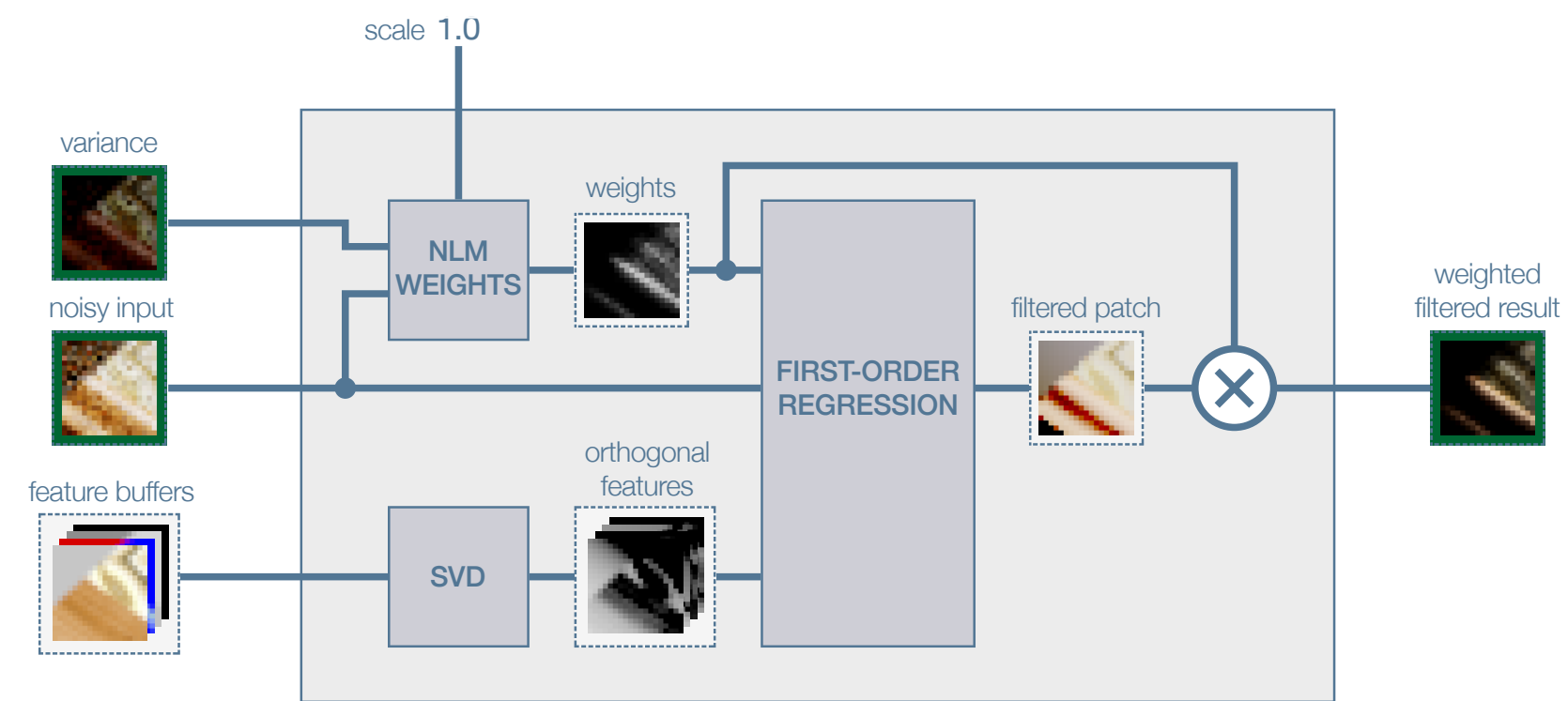
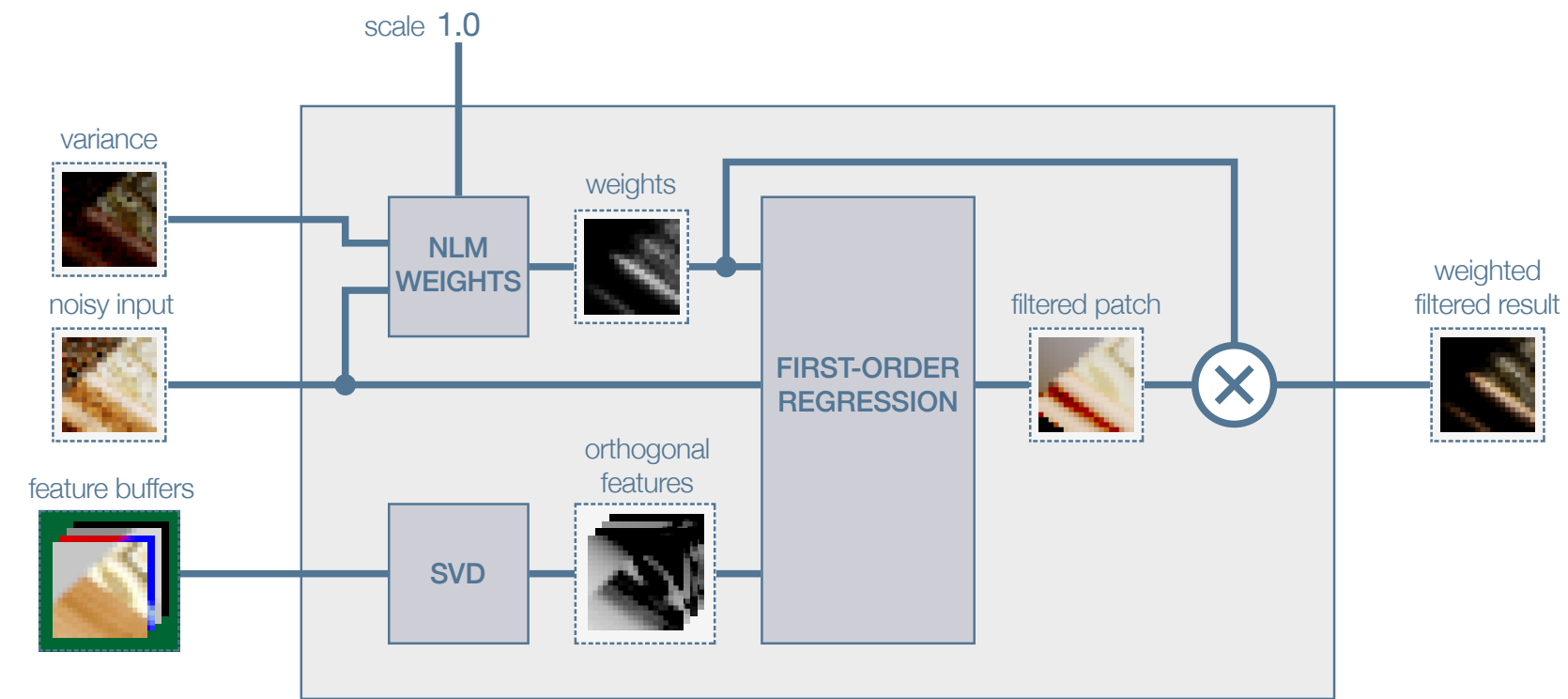


# Algorithm Overview



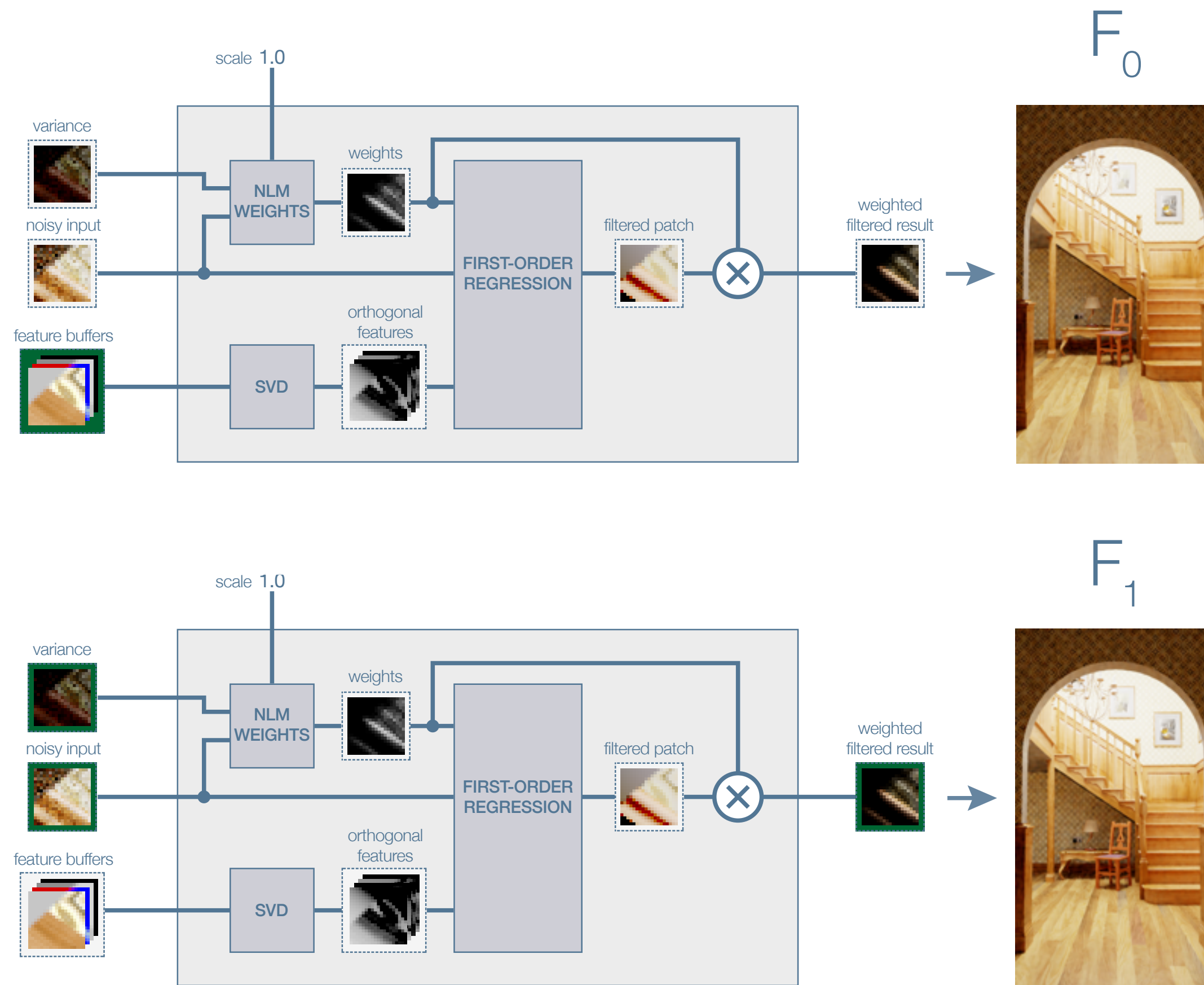


# Algorithm Overview



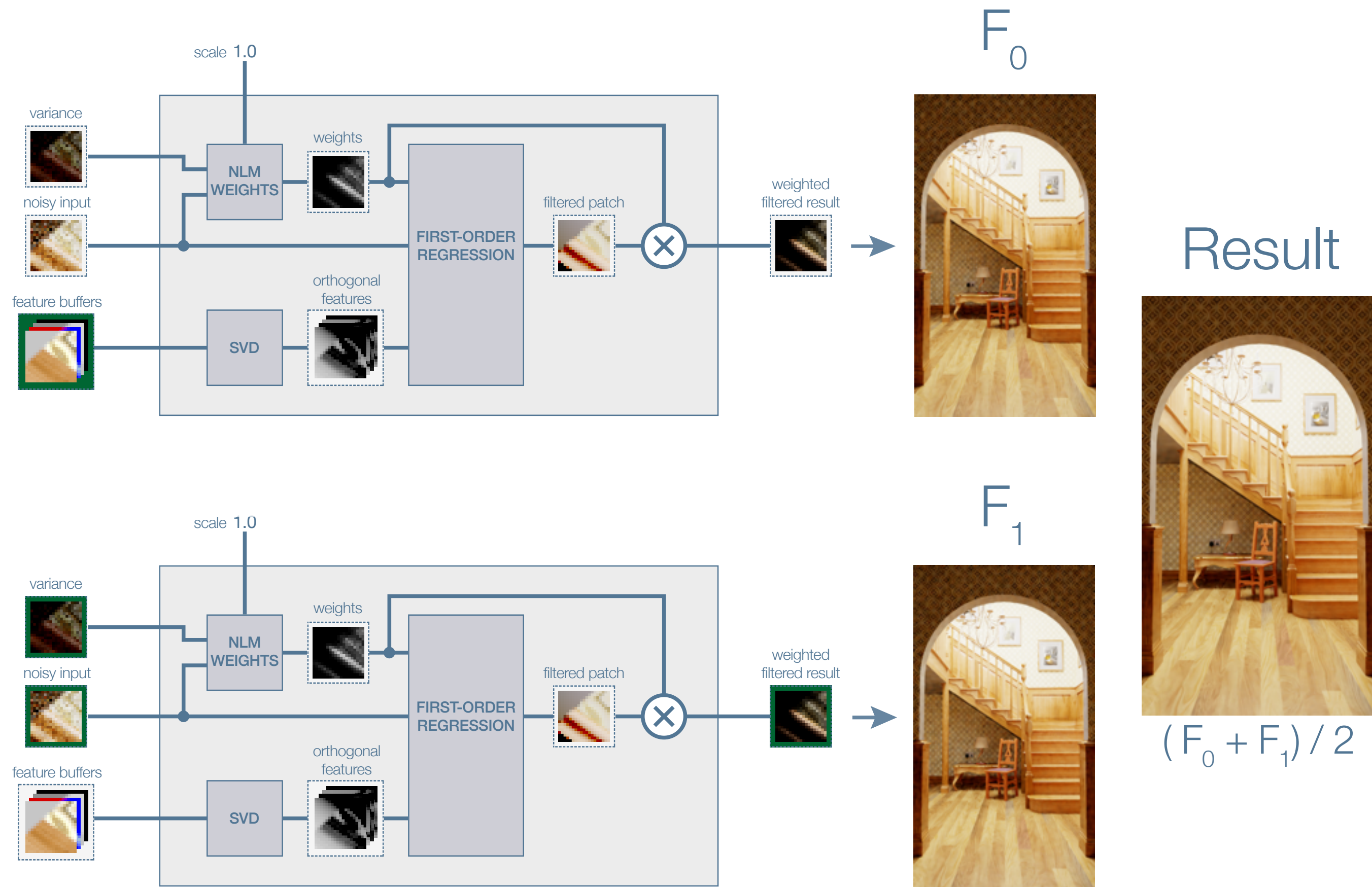


# Algorithm Overview



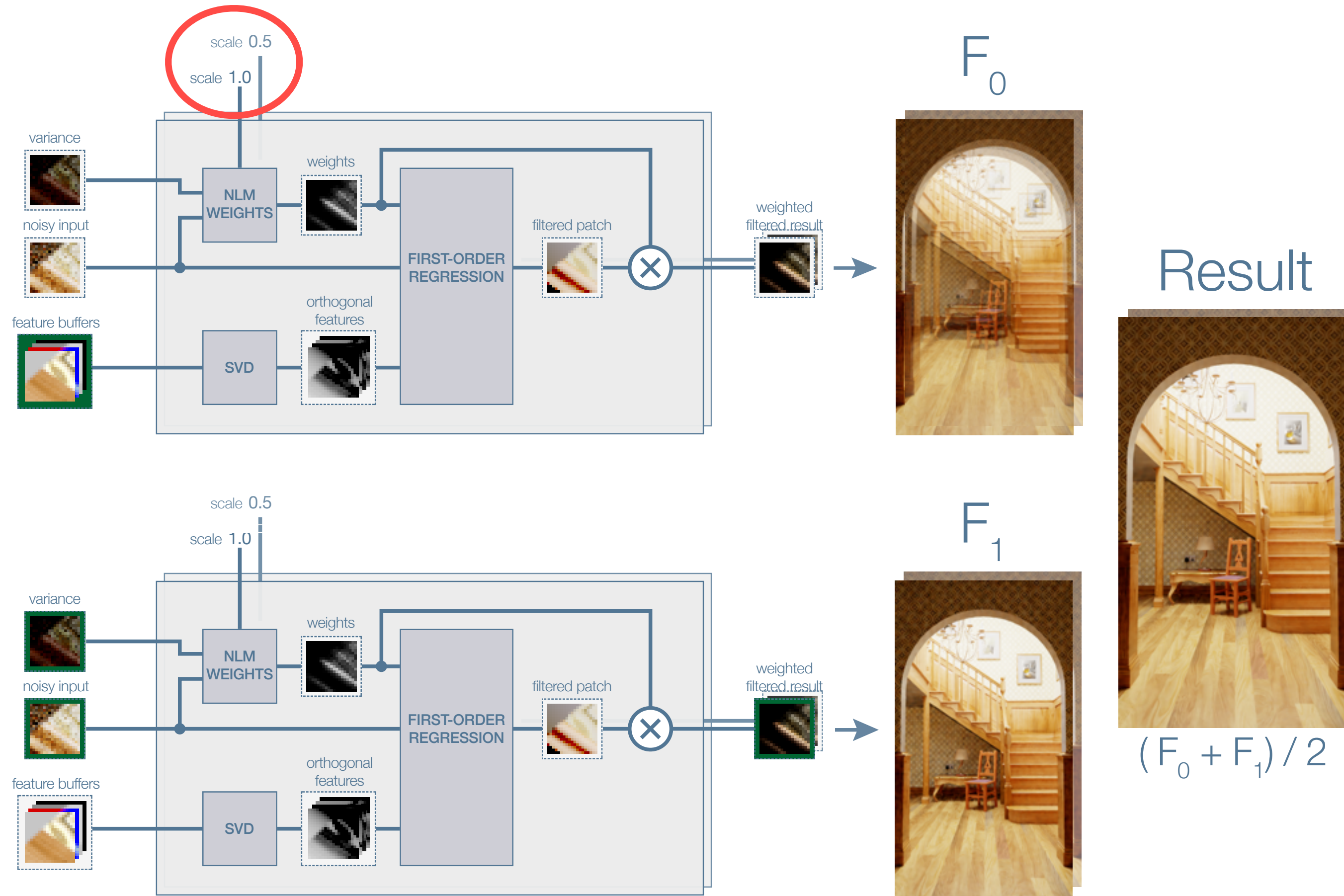


# Algorithm Overview



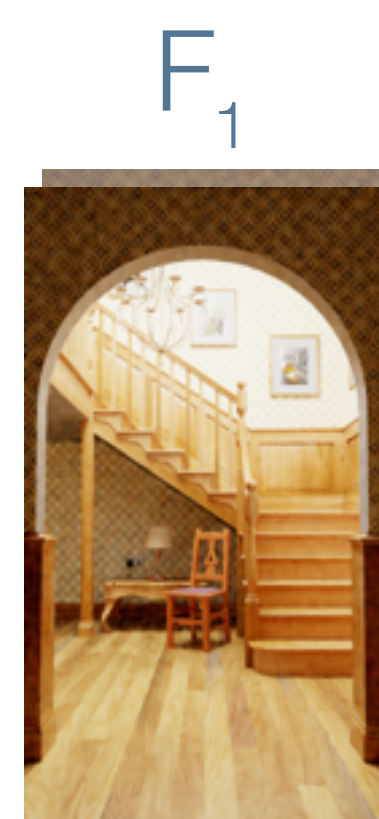
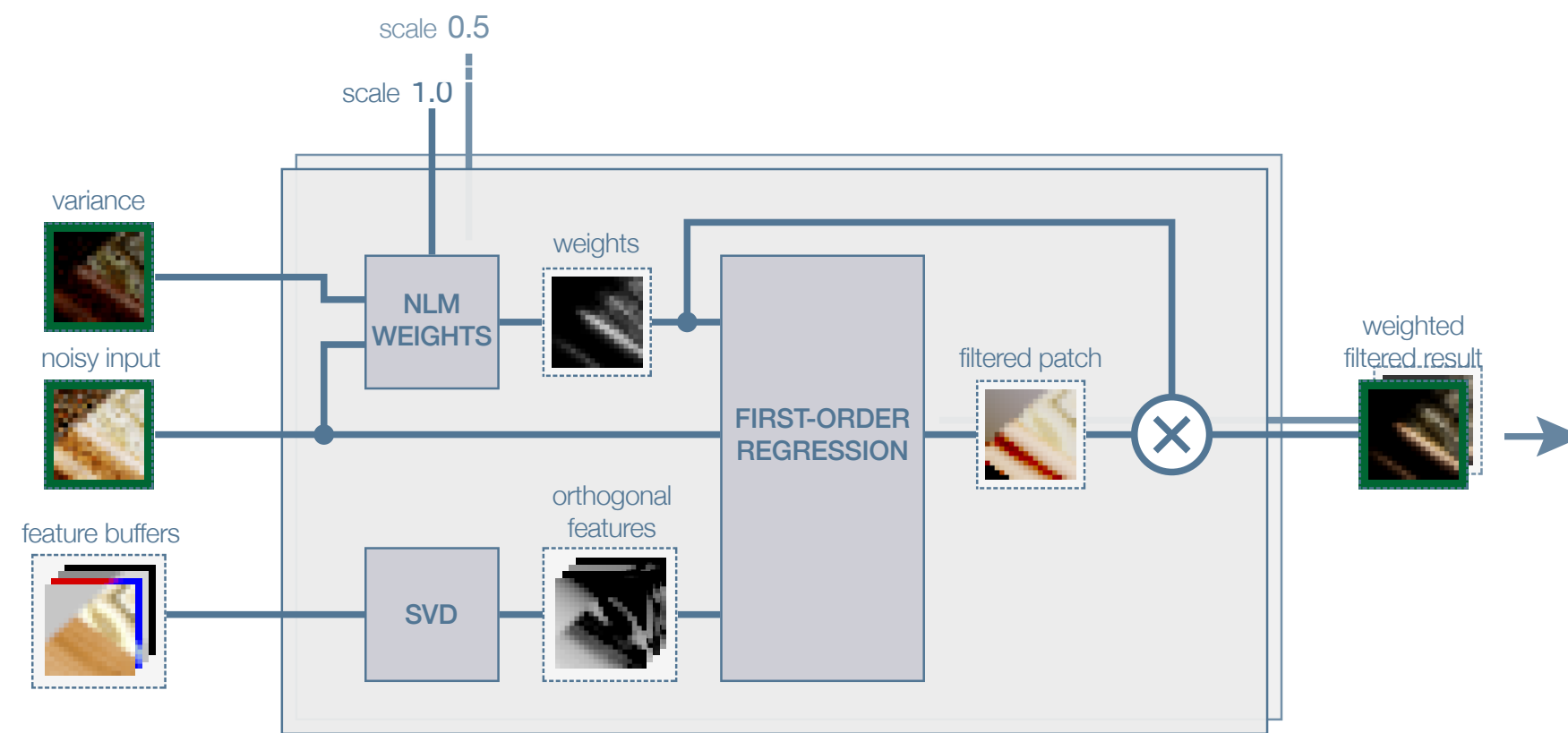
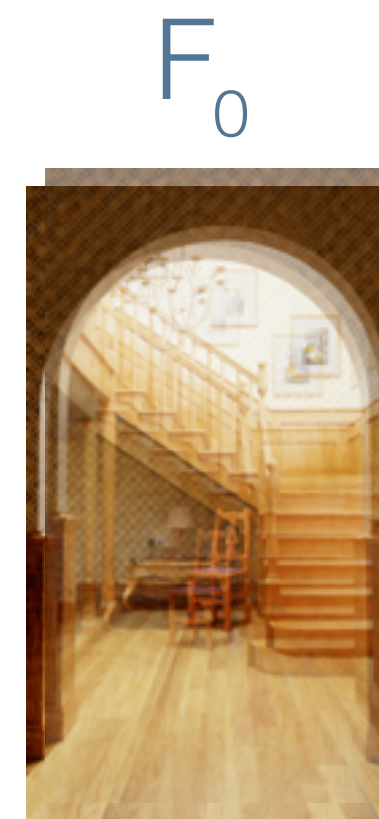
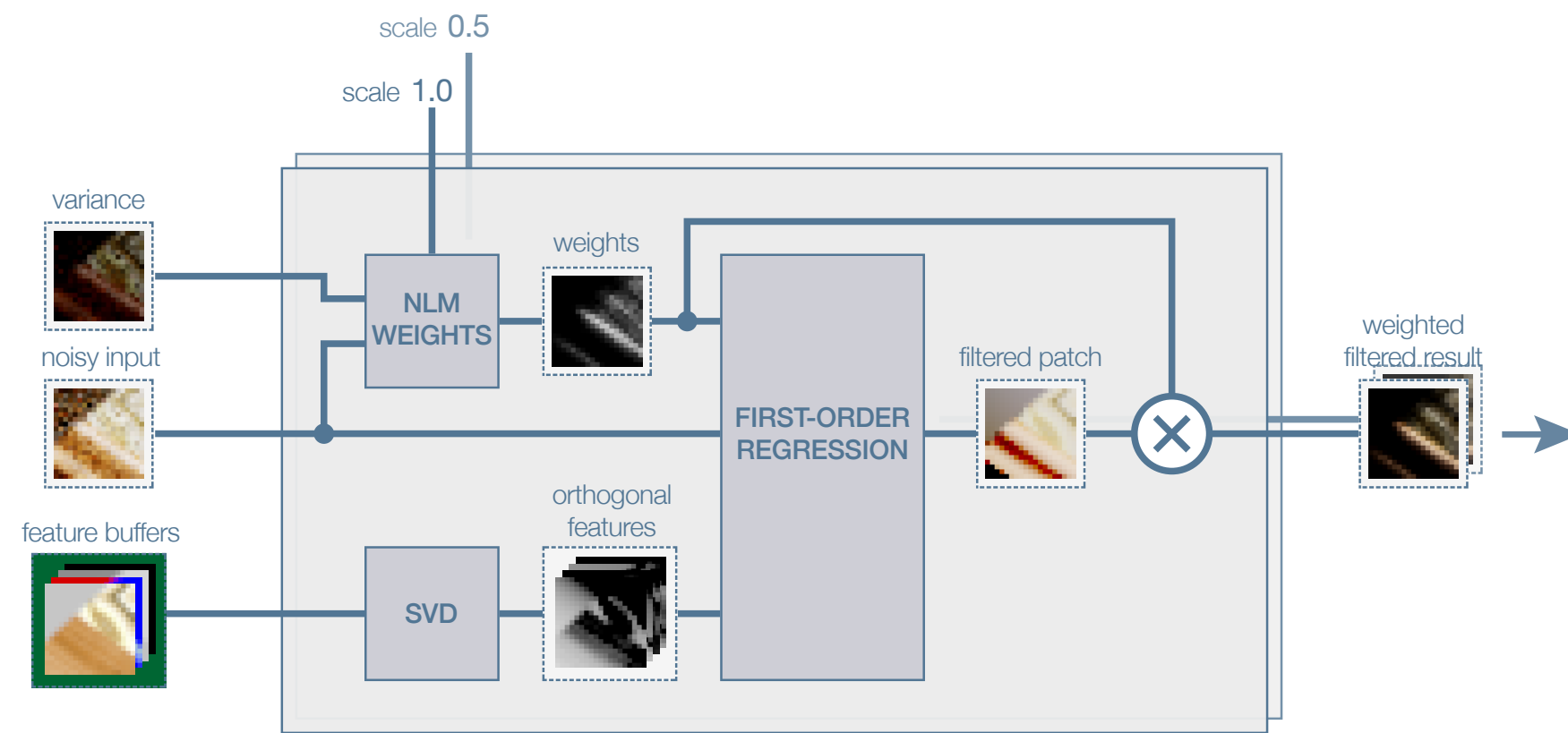


# Algorithm Overview





# Algorithm Overview



Result



$$(F_0 + F_1) / 2$$

Scale selection  
→



First filtering pass



# Algorithm Overview



First  
filtering  
pass

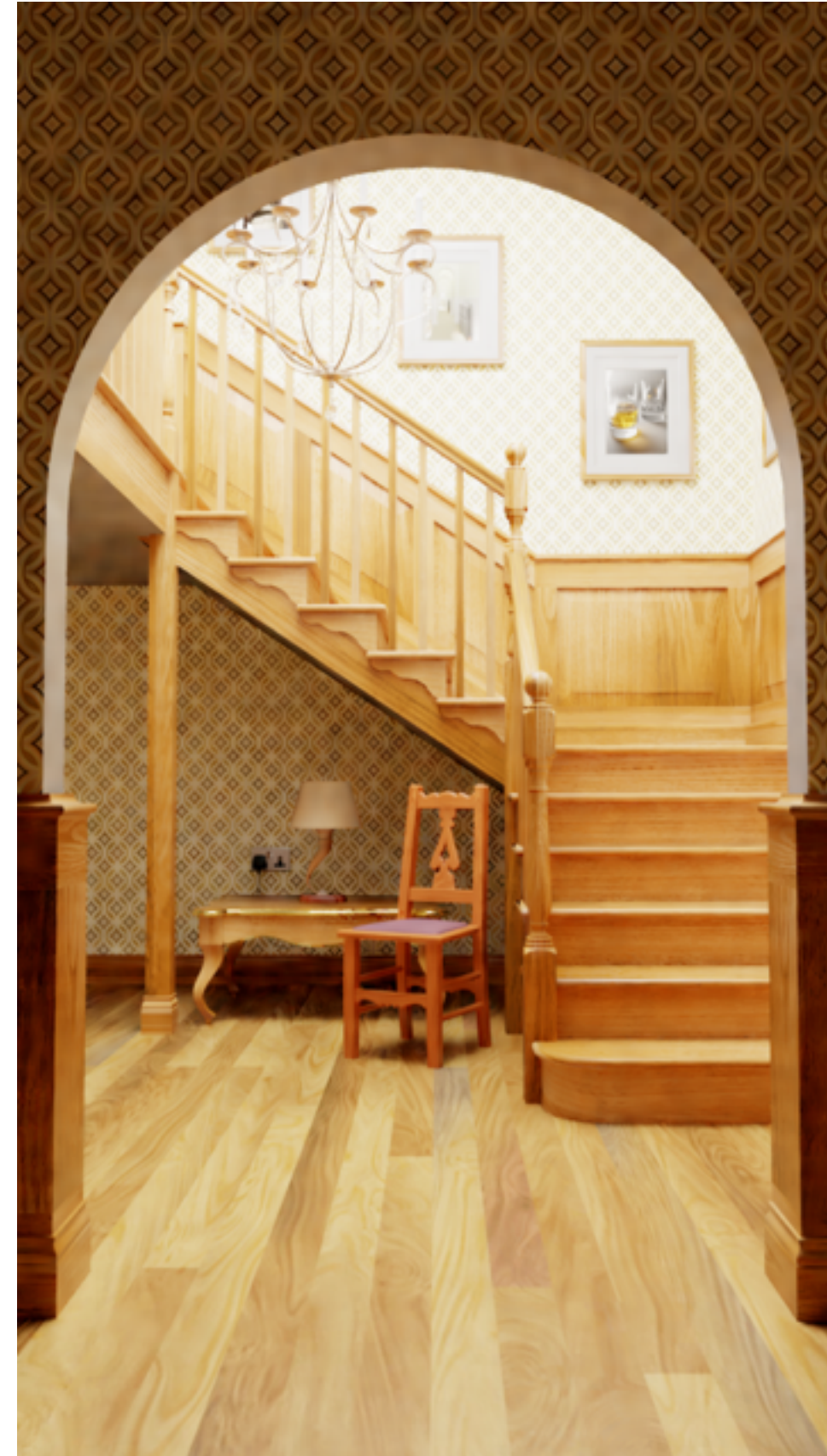




# Algorithm Overview



First  
filtering  
pass



Second  
filtering  
pass



≠  
first  
pass



# Results

<http://drz.disneyresearch.com/~jnovak/publications/NFOR/supplementary/index.html>





16 spp 64 spp 256 spp 1024 spp

Color buffers Structural Dissimilarity rMSE Heatmap

1: Input 2: NLM 3: NLM-MS 4: RHF 5: RDFC 6: LBF 7: WLR 8: WLR-PF 9: NFOR (ours) 10: Reference





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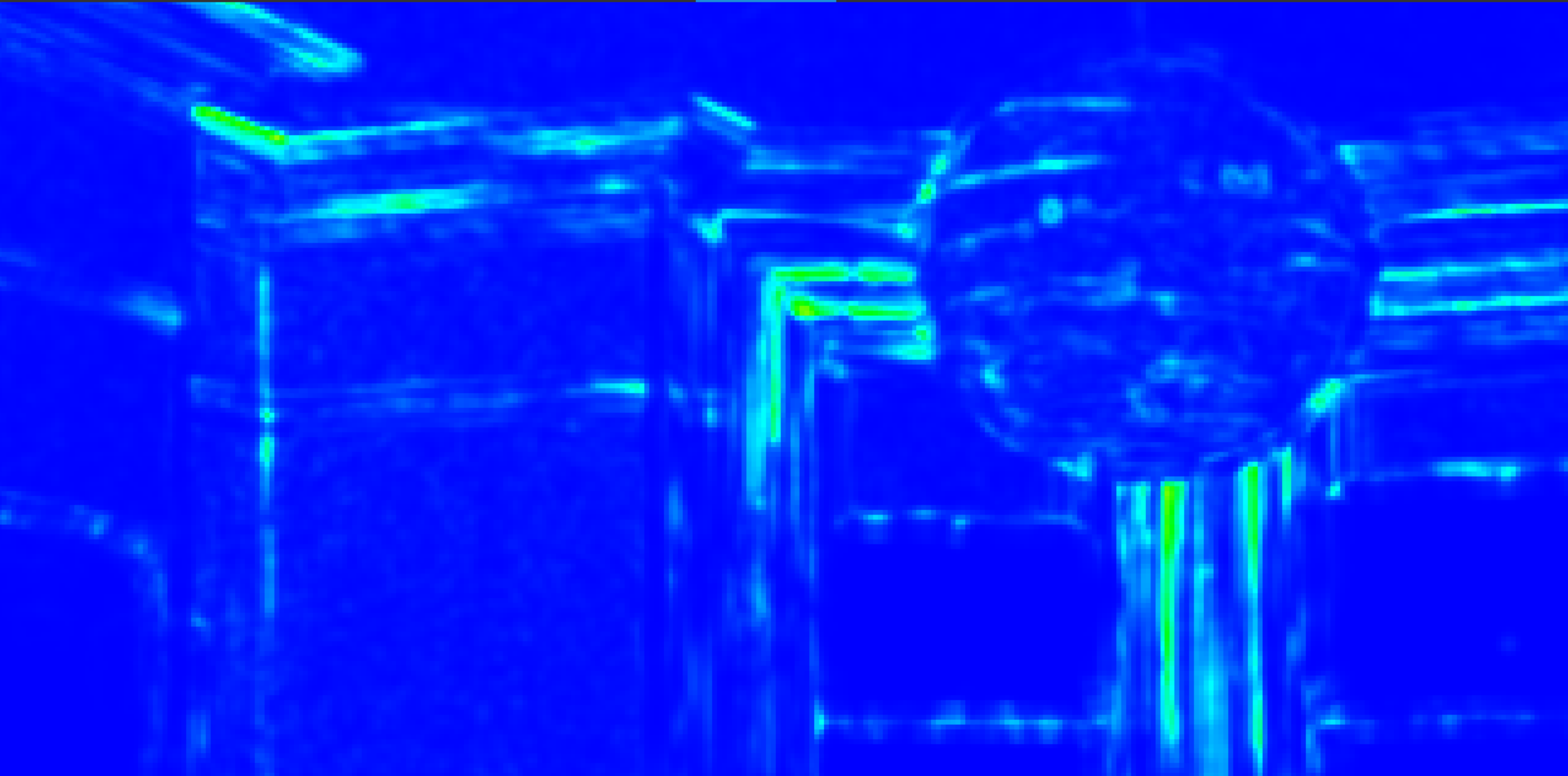




16 spp   64 spp   256 spp   1024 spp

Color buffers   Structural Dissimilarity   rMSE Heatmap

1: Input   2: NLM   3: NLM-MS   4: RHF   5: RDFC   6: LBF   7: WLR   8: WLR-PF   9: NFOR (ours)

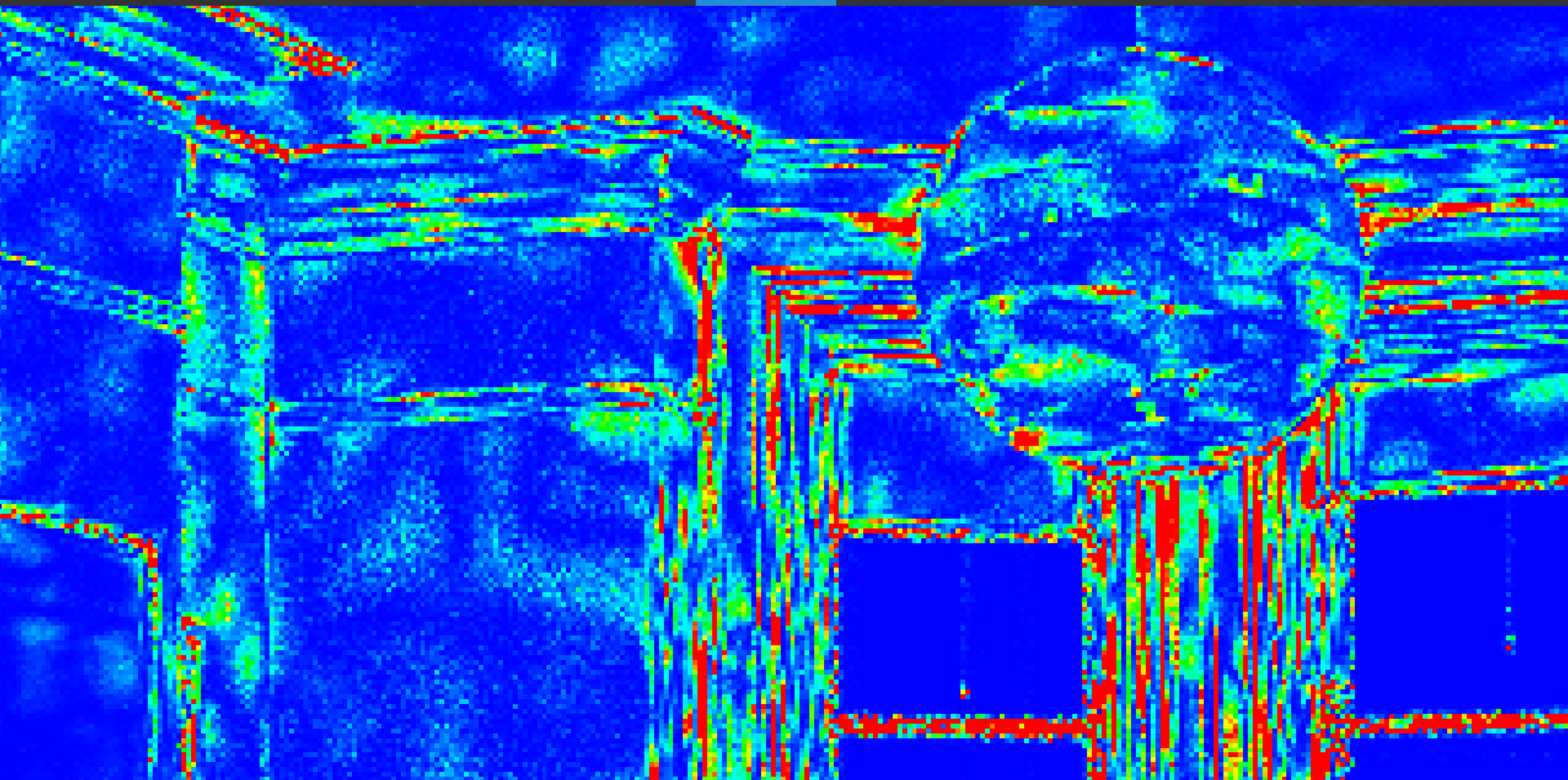




16 spp 64 spp 256 spp 1024 spp

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1: Input 2: NLM 3: NLM-MS 4: RHF 5: RDFC 6: LBF 7: WLR 8: WLR-PF 9: NFOR (ours)





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Color buffers Structural Dissimilarity rMSE Heatmap

1: Input 2: NLM 3: NLM-MS 4: RHF 5: RDFC 6: LBF 7: WLR 8: WLR-PF 9: Ours 10: Reference





16 spp 64 spp 256 spp 1024 spp

Color buffers Structural Dissimilarity rMSE Heatmap

1: Input 2: RenderMan Denoiser 3: RenderMan Denoiser 21.0b1 4: NFOR (ours) 5: Reference





16 spp 64 spp 256 spp 1024 spp

Color buffers Structural Dissimilarity rMSE Heatmap

1: Input 2: RenderMan Denoiser 3: RenderMan Denoiser 21.0b1 4: NFOR (ours) 5: Reference



16 spp 64 spp 256 spp 1024 spp

Color buffers Structural Dissimilarity rMSE Heatmap

1: Input 2: RenderMan Denoiser 3: RenderMan Denoiser 21.0b1 4: NFOR (ours) 5: Reference





16 spp 64 spp 256 spp 1024 spp

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1: Input 2: RenderMan Denoiser 3: RenderMan Denoiser 21.0b1 4: NFOR (ours) 5: Reference



16 spp 64 spp 256 spp 1024 spp

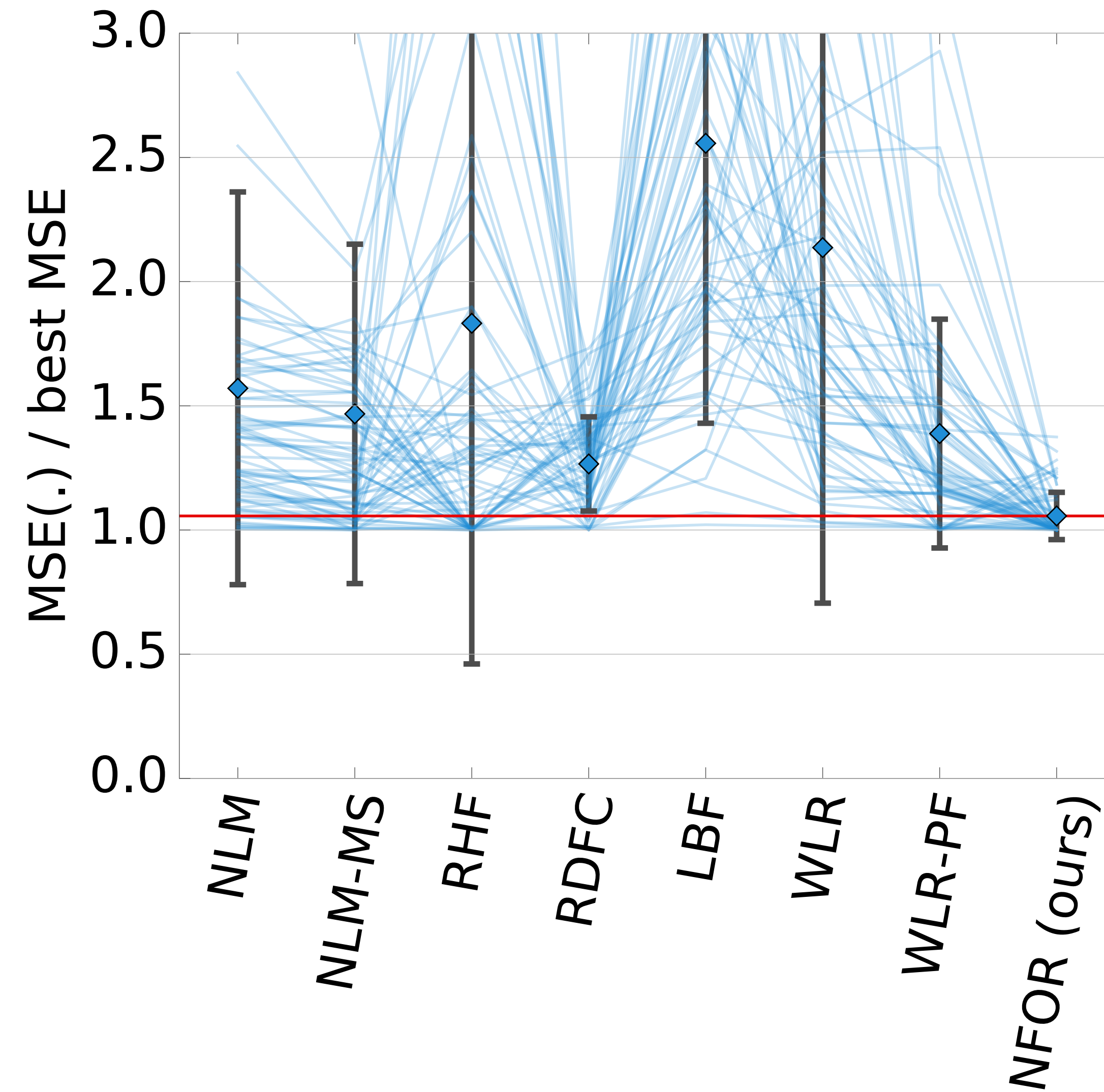
Color buffers Structural Dissimilarity rMSE Heatmap

1: Input 2: RenderMan Denoiser 3: RenderMan Denoiser 21.0b1 4: NFOR (ours) 5: Reference

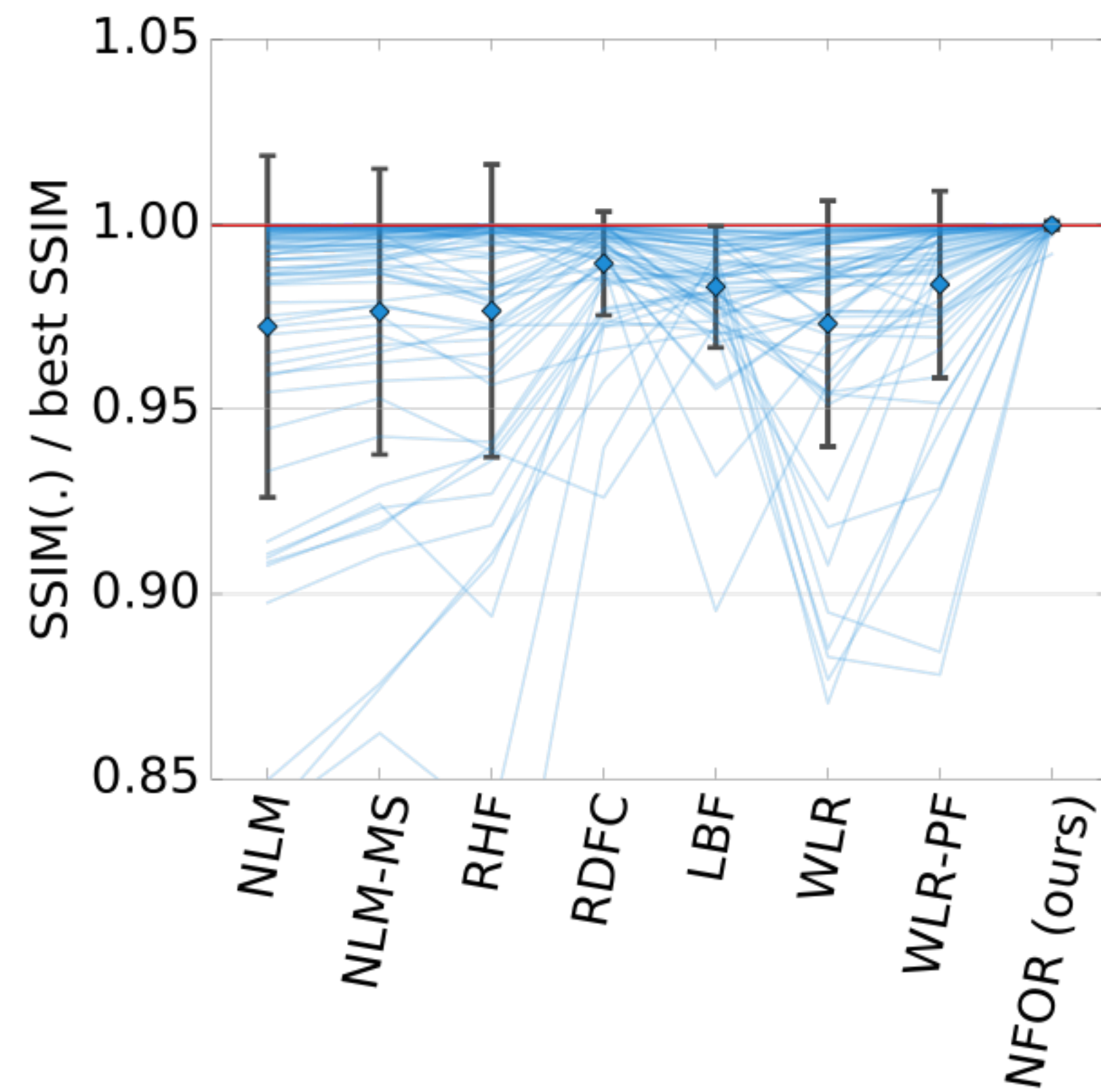
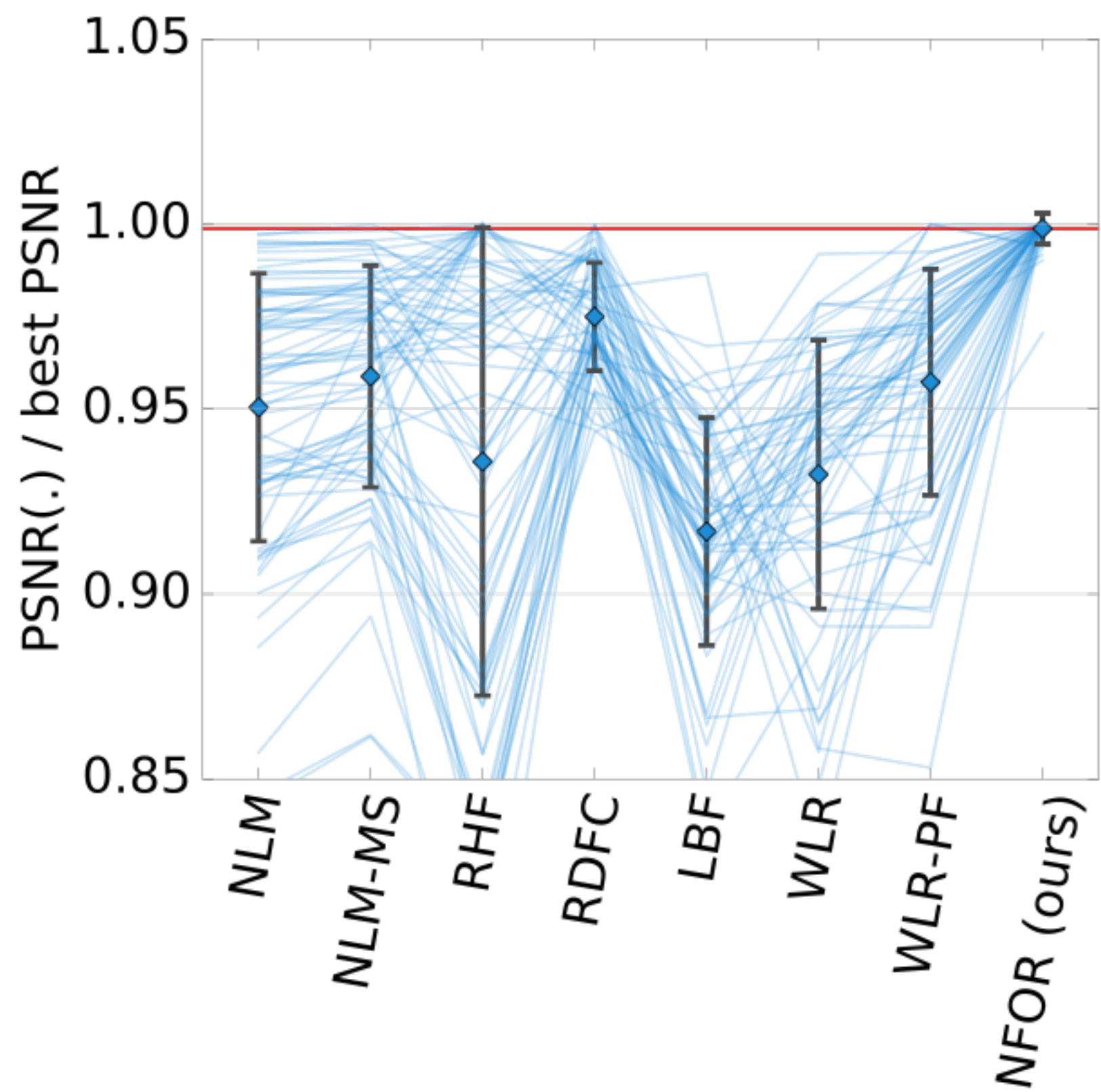
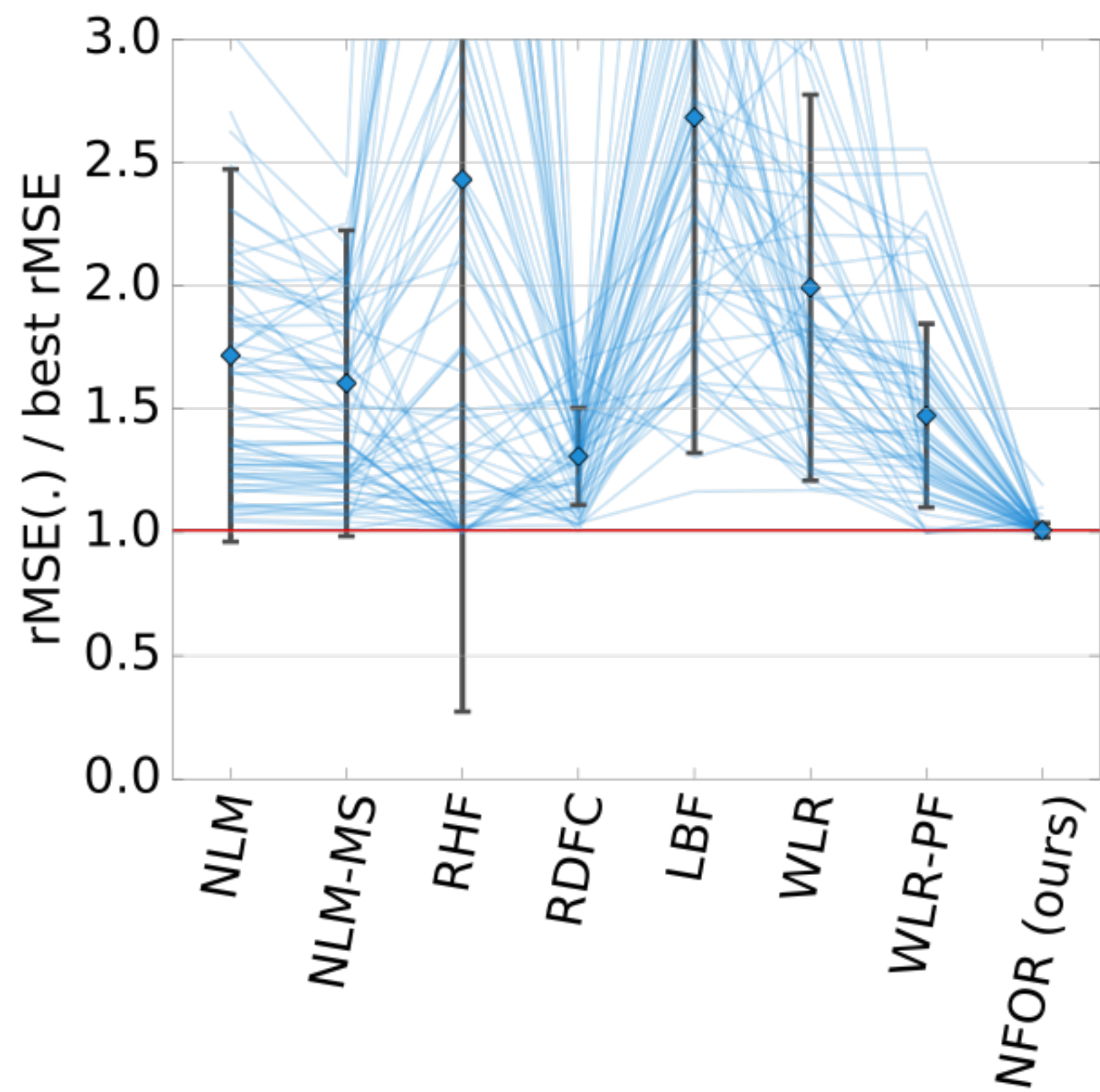




# Error Metrics



# Error Metrics





# Limitations

No adaptive sampling (yet)

High overhead

Algorithm	Avg. Runtime	Avg. Memory Usage
RDFC	41s	349 MB
RHF	18s	460 MB
WLR	72s	309 MB
WLR-PF	91s	311 MB
NFOR (ours)	223s	3248 MB

# Conclusion

Comparative analysis of recent denoising techniques

Novel filter with state-of-the-art results

Future work

Comparative analysis of adaptive sampling techniques

Sparse reconstruction to reduce overhead



Input



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